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# Technical Report

524

## Theory and Operating Characteristics of TRAPATT Amplifiers

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26 January 1977

Prepared for the Ballistic Missile Defense Program Office,  
Department of the Army,  
under Electronic Systems Division Contract F19628-76-C-0002 by

### Lincoln Laboratory

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

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THEORY AND OPERATING CHARACTERISTICS  
OF TRAPATT AMPLIFIERS

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TECHNICAL REPORT 524

26 JANUARY 1977

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### ABSTRACT

This report describes the current state of understanding of the theory and operating characteristics of microwave avalanche diodes operating in the TRAPATT mode as both oscillators and amplifiers. Device operating principles, and their dependence upon material, impurity profile, structure, biasing, and circuit loading are described. Methods of device fabrication are discussed, and present state of the art is tabulated for oscillators and amplifiers on a power-frequency basis.

Techniques developed for the design of TRAPATT amplifiers as a result of several programs sponsored by the U.S. Army Ballistic Missile Defense Advanced Technology Center are discussed, and experimental results (primarily at S-band) are presented.

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# THEORY AND OPERATING CHARACTERISTICS OF TRAPATT AMPLIFIERS

## CHAPTER I HISTORICAL BACKGROUND

### A. INTRODUCTION

The purpose of this report is to document the present state of understanding of the theory and operating characteristics of TRAPATT diodes. The discovery of this mode of oscillation in solid-state devices in the late 1960's generated interest and support on the part of the Ballistic Missile Defense (BMD) technology development community, since peak power levels, efficiencies, and operating frequencies of these devices are compatible with requirements for S-band phased-array-radar power amplifiers.

This chapter discusses the discovery of the TRAPATT phenomena in a historical sense, and relates it to transit-time negative resistance and the IMPATT diode of Shockley<sup>1</sup> and Read,<sup>2</sup> respectively.

Chapters II through IV then develop the theoretical concepts responsible for the operation of the device, describe various methods available for its fabrication, and tabulate the present oscillator and amplifier state of the art.

Chapters V and VI discuss techniques for the design of TRAPATT amplifiers and provide experimental results which are characteristic of the best of those which have been constructed.

Chapter VII summarizes this report and provides conclusions and further recommendations, and the Appendix presents a bibliography of Government Contract Reports available from the National Technical Information Service (NTIS) concerning TRAPATT generation and amplification of microwave power.

### B. DISCOVERY AND DESCRIPTION OF THE IMPATT MODE

The negative resistance arising from the transit time of charge carriers in semiconductor devices was first considered by Shockley<sup>1</sup> in 1954. The device proposed by Shockley was a pnp structure in which charge carriers are injected at one of the p-n junctions and drift through the n-region to the opposite junction. Because a finite time is required for the particles to traverse the structure, the terminal current induced by the moving charge carriers lags the terminal voltage by the transit time of the injected particles. For appropriate frequencies, the phase difference between the terminal current and voltage remains between 90° and 270°. Therefore, the device exhibits a negative resistance and is capable of generating RF power. Shockley proposed that these devices be used as amplifiers.

A diode structure in which the phase lag between the terminal current and voltage is achieved by both: (1) generation of charge carriers through impact ionization, and (2) the transit time of these carriers, was proposed by Read<sup>2</sup> in 1958. The structure proposed by Read was an  $n^+p$  diode in which the electric field at the  $n^+p$  junction would be large enough to allow charge multiplication by impact ionization. (Throughout this report, the + superscript refers to a highly doped, or low-resistivity region of semiconductor material.) The p-region is made narrow so that most of the charge multiplication occurs at the  $n^+p$  interface. The electric field in the

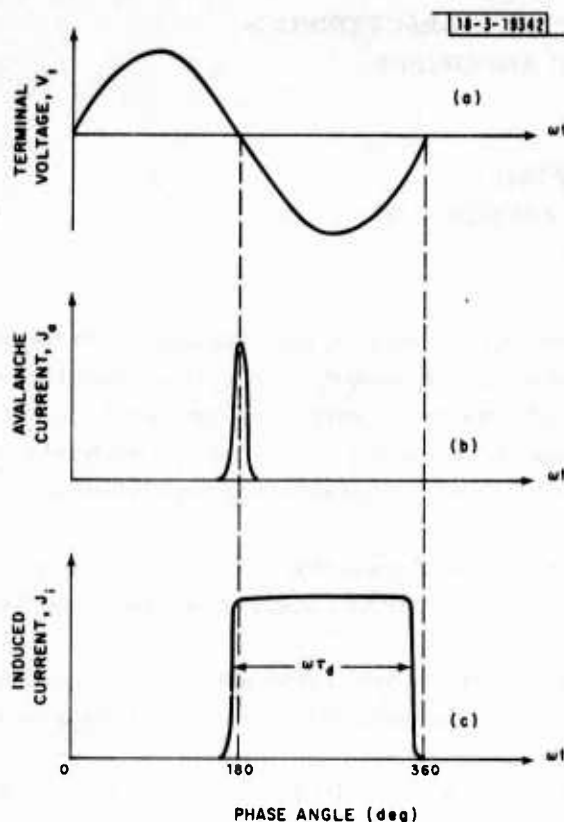


Fig. I-1. IMPATT mode waveforms.

intrinsic region is not large enough to sustain avalanche multiplication but is high enough so that the injected charge carriers travel at field-independent, saturated velocities. The avalanche multiplication process contributes a  $90^\circ$  inductive phase lag to the terminal current-voltage waveforms (e.g., see Fig. I-1) and the transit time of the charge carriers contributes an additional phase delay so that the current induced in the external circuit lags the voltage by a phase angle between  $90^\circ$  and  $270^\circ$ . The device, therefore, produces a negative resistance. Read showed theoretically that the device was capable of producing high-power microwave oscillations with efficiencies of 30 percent. This mode of oscillation was given the acronym IMPATT mode (impact ionization avalanche transit time) and has been discussed extensively in the literature. Experimentally, IMPATT oscillations have been observed in both p-n junction diodes and Read-type structures. Diodes operating in the IMPATT mode usually have a cutoff frequency, below which the phase delay of the current relative to the voltage is less than  $90^\circ$  and, therefore, the diode does not possess negative resistance. Typical power levels and efficiencies for this mode of operation are generally less than 3 or 4 W at X-band, and 10- to 15- percent efficiency for the simpler p-n junction diodes, and up to 37-percent<sup>3</sup> efficiency for structures similar to that proposed by Read.

### C. DISCOVERY OF THE HIGH-EFFICIENCY MODE

In 1967, Prager *et al.*,<sup>4</sup> while using Si avalanche diode oscillators, observed a new high-efficiency mode of operation that differed considerably from the usual IMPATT operation. The new mode was characterized by efficient DC-to-RF conversions (up to 60 percent), operation at frequencies well below the IMPATT transit-time cutoff frequency, and a significant change

in the DC voltage when the diode switched into the mode. Since this new mode did not obey the IMPATT explanations they called their discovery the "anomalous mode."

In 1968, Scharfetter et al.<sup>5</sup> proposed a mechanism for this new mode which they called the TRAPATT mode (an acronym for trapped plasma avalanche triggered transit). Their explanation was based on a detailed computer simulation of an avalanche diode and showed the formation of a moving avalanche zone and trapped plasma.<sup>6</sup> Based on the computer results, DeLoach and Scharfetter<sup>7</sup> proposed a simplified analysis of the device physics of the TRAPATT mode mechanism. A similar explanation was offered at approximately the same time by Clorfeine et al.<sup>8</sup> The simplified analyses usually proceed by assuming a particular current waveform across the diode (e.g., a square wave) and then calculating the corresponding voltage waveform from the device physics. A Fourier analysis of the waveforms is then performed so that impedances, efficiencies, and other important operating parameters of the device can be calculated.

## CHAPTER II THEORY OF DEVICE OPERATION

### A. BASIC OPERATING PRINCIPLES

The diodes used for TRAPATT mode applications can have a variety of doping profiles including the  $n^+pp^+$ ,  $n^+npp^+$ , or  $p^+nn^+$  structures. When reverse biased into avalanche breakdown, these have doping and electric field profiles similar to that shown in Fig. II-1 for the  $n^+pp^+$  diode. In contrast to most IMPATT devices, the diodes used for TRAPATT mode applications are "punched through" under reverse bias and, thus, the whole lightly doped region is depleted of carriers. Any undepleted region is undesirable because it acts as a series resistance to the diode and although it has a stabilizing effect on oscillator performance, it has a strong degrading effect on the oscillator RF power and efficiency. As will be seen later, a high punch-through factor (i.e., lower doping in the p-layer) is generally desirable for efficient TRAPATT operation.

For an understanding of the operating principles of the TRAPATT mode, it is useful to assume a square-wave terminal current through the diode so that a constant amplitude current with a relatively high magnitude flows for one-half the RF cycle and a constant amplitude current with a low magnitude flows for the second half of the RF cycle. The current flowing through

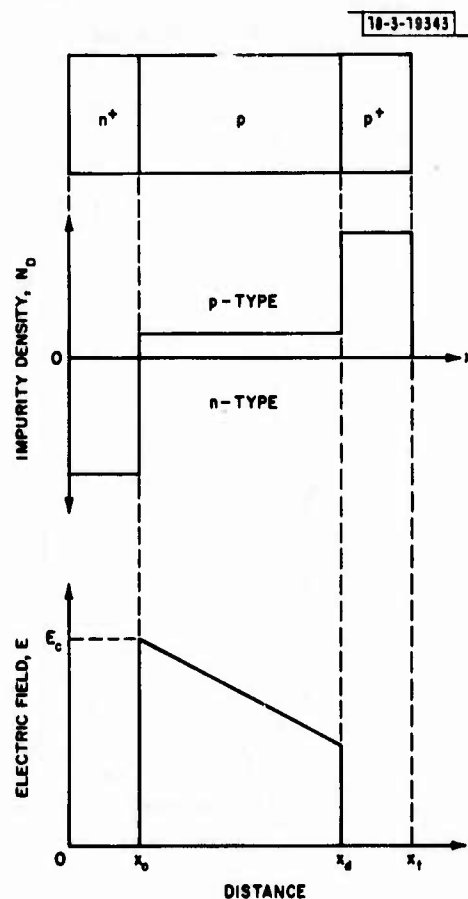


Fig. II-1. TRAPATT diode impurity density and electric field profiles.

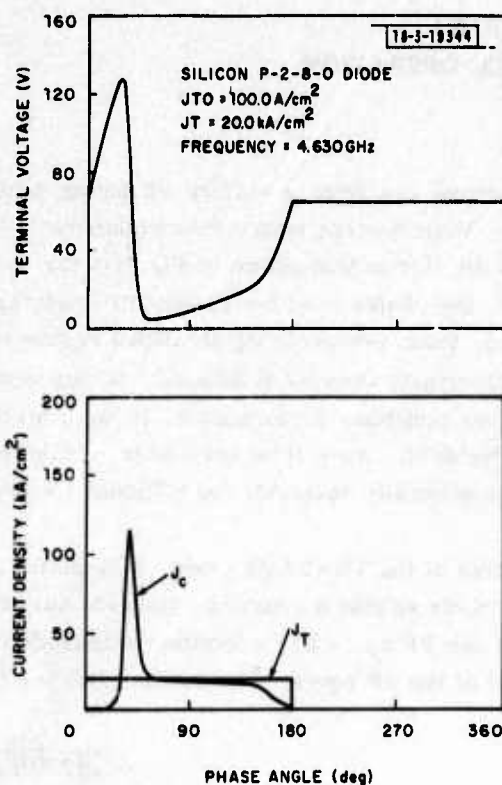


Fig. II-2. TRAPATT diode terminal waveforms.

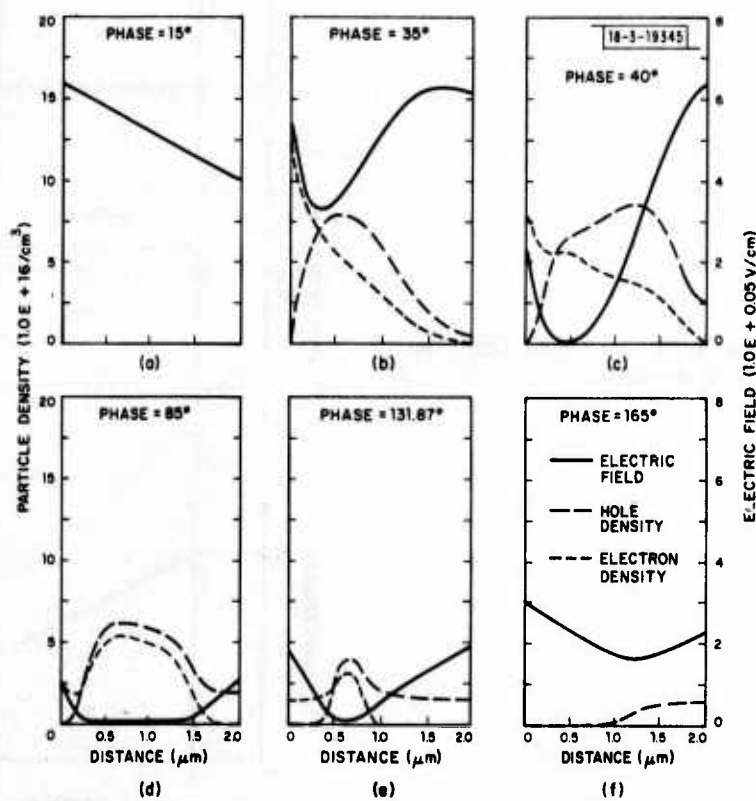


Fig. II-3. TRAPATT profiles during oscillation cycle.



the diode during the second half of the cycle or "off" period can be considered to be the reverse saturation current in this situation. The terminal voltage and current waveforms under these conditions are illustrated in Fig. II-2.

The internal dynamics of the TRAPATT mode are illustrated in Figs. II-3(a-f) for selected times during the first half of the RF cycle.

Initially, the diode voltage is assumed to be just below the breakdown value so that only a small reverse saturation conduction current  $J_C$  flows. The constant magnitude terminal current  $J_T$  is suddenly applied, causing a displacement current to charge the diode as a linear capacitor [Fig. II-3(a)]. Under these conditions the terminal current is primarily composed of that displacement current. As the diode charges, the voltage rises in proportion to the integral of the terminal current and when the voltage becomes larger than the breakdown value, an electron-hole plasma is generated in the diode [Fig. II-3(b)]. This process continues until enough charge has been generated so that the terminal current is entirely composed of conduction current. The space charge from the generated carriers is sufficient to force the electric field on the right of the avalanche zone to a high enough value so that additional charge carriers are generated. As this occurs, a "shock front" or traveling avalanche zone is created in which the electric field to the right of the zone is increased above the breakdown field and a dense electron-hole plasma is left in the "wake" of the traveling zone [Fig. II-3(c)]. The electron-hole plasma reduces the electric field behind the avalanche zone to a small value. The avalanche zone propagates rapidly so that the electron-hole plasma, which now drifts at low, electric-field-dependent velocities, is not able to catch up. As a result, the diode is filled with the trapped plasma and the terminal voltage is reduced to a minimum value [Fig. II-3(d)].

Since the terminal current is maintained at a constant value, the plasma is drained from the diode at low, field-dependent velocities. The holes drift to the right toward the  $p^+$ -contact and the electrons to the left toward the  $n^+$ -contact. As the charge carriers are drained from the regions adjacent to the highly doped contacts, the electric field in these regions begins to recover and increase in magnitude [Fig. II-3(e)]. This process continues until the diode is completely drained of mobile charge carriers [Fig. II-3(f)]. The diode again acts as a linear capacitor and the voltage increases in proportion to the integral of the terminal current. This process continues until the diode terminal voltage reaches a value just below the breakdown condition and the half-cycle is complete. A Fourier analysis now can be made on the terminal current and voltage waveforms to determine RF power, efficiency, impedances, etc.

High efficiencies are possible with the TRAPATT mode because the RF cycle consists of a high-current low-voltage condition for the first half of the RF period and a high-voltage low-current condition for the second half of the RF period. The diode, simply stated, acts as a microwave switch.

It should be clear from the current and voltage waveforms that the operating voltage in the TRAPATT mode is much lower than the breakdown voltage of the device. It has been observed that, in general, the lower the operating voltage relative to the breakdown voltage, the more efficient the device will be.

The waveforms shown in Figs. II-2 and -3 represent the final steady-state oscillations in the device. They were obtained from a computer analysis developed by Lee *et al.*<sup>9,10</sup> and results on various types of structures based on this analysis are given elsewhere.<sup>11</sup>

This analysis assumes a square current waveform, which Bryant and Welch<sup>12</sup> have shown is not accurate since it requires power to be supplied to the diode at higher harmonics of the

oscillator waveform. Other analyses<sup>13,14</sup> reveal that high-efficiency waveforms do exist which satisfy requirements for trapped plasma formation and field-dependent extraction without a requirement for active harmonic terminations. The analysis does contain the appropriate semiconductor physics constraints, and is believed to provide an accurate basis for comparing different device structures and materials.

Finally, transient starting mechanisms for the TRAPATT mode are discussed in Sec. D.

## B. APPROXIMATE ANALYSIS

Several simple approximate analyses exist, which provide basic information concerning the device principles and properties. One of these has been presented by Haddad *et al.*,<sup>15</sup> based on previous work done by Schroeder and Haddad<sup>16</sup> (avalanche-region width), Evans<sup>17</sup> (approximate expression for the delay time and overvoltage), and DeLoach and Scharfetter<sup>7</sup> (recovery time after the initiation of the dense plasma). Most of the important features of the TRAPATT mode can be readily seen from this model.

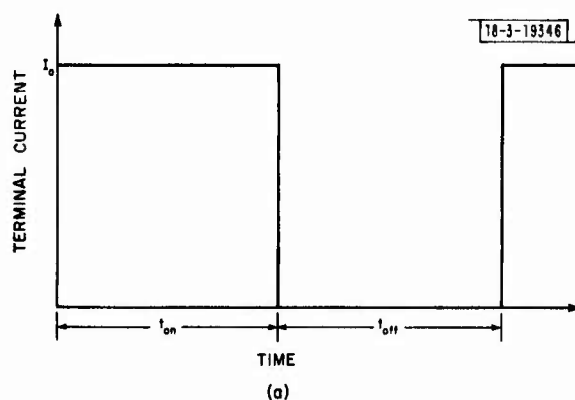
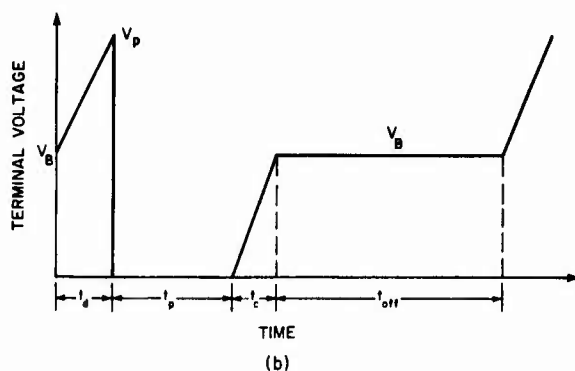


Fig. II-4(a-b). Approximate current and voltage waveforms.



In this analysis the terminal current of the diode is assumed to have the waveform shown in Fig. II-4(a), and the corresponding terminal voltage is approximated by the waveform shown in Fig. II-4(b) where

- $t_d$  = delay time
- $t_p$  = recovery time
- $t_c$  = diode charging time

$t_{on}$  = "on" time

$t_{off}$  = "off" time.

The diode terminal voltage at the beginning of the cycle is chosen to be the diode DC breakdown voltage  $V_B$ . The "on" time  $t_{on}$  is chosen to be  $t_{on} = t_d + t_p + t_c$ , and the "off" time  $t_{off}$  is chosen to be equal to  $t_{on}$ . The waveform shown in Fig. II-4 is idealized but gives reasonable results at the fundamental frequency and has been employed by others.<sup>7,8,12</sup> Since  $t_{on}$  is assumed to equal  $t_{off}$ , the fundamental frequency is given by  $f = 1/2t_{on}$ .

For the analysis, the breakdown voltage  $V_B$  and the avalanche region width  $\bar{w}$  for a particular diode structure are obtained as described by Schroeder and Haddad.<sup>16</sup> Then the delay time  $t_d$  and the peak voltage  $V_p$  are calculated by solving Evans<sup>17</sup> equations which are given by

$$t_d = \frac{\epsilon}{\lambda J_o} \ln \left[ 1 + \frac{\lambda J_o}{\epsilon} \left( t_d + \frac{\bar{w}}{2v_s} \ln \frac{J_o}{J_s} \right) \right] \quad (II-1)$$

and

$$V_p = V_B + \frac{wJ_c}{\epsilon} t_d, \quad (II-2)$$

where  $\lambda$  = the constant in  $\alpha = A_o \exp[\lambda E]$ . For silicon, the value of  $\lambda$  has been chosen<sup>5</sup> to be  $0.333 \times 10^{-5}$  cm/V,

$J_o$  = total current density during the first half-cycle,

$J_s$  = reverse saturation current density (a value of 1 A/cm<sup>2</sup> is taken for  $J_s$  in this study),

$\bar{w}$  = avalanche region width, defined as the width where the majority particle current density reaches 85 percent of the total current density when the diode is reverse biased into breakdown,

$w$  = diode width, and

$v_s$  = saturated drift velocities of carriers ( $v_s$  is assumed to be  $1 \times 10^7$  cm/sec in this study).

The recovery time  $t_p$  is obtained by using DeLoach and Scharfetter's<sup>7</sup> equation

$$t_p = \frac{w}{2v_p} + \frac{w}{2v_s}, \quad (II-3)$$

where

$$v_p = v_s \frac{J_o}{J_p} \quad (II-4)$$

and  $J_p$  is obtained by solving

$$\frac{J_p}{J_s} = \exp \left[ \frac{J_p}{J_o} \right]. \quad (II-5)$$



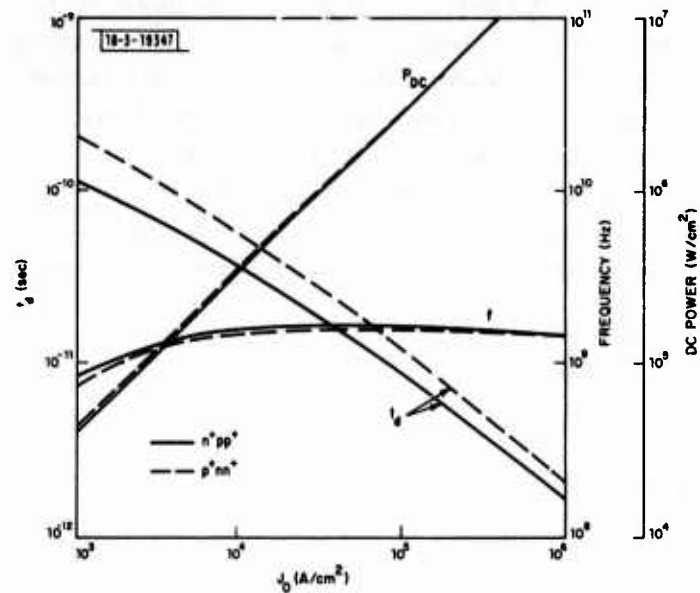


Fig. II-5. Dependence of power, frequency, and delay time on current density for n- and p-type diodes.

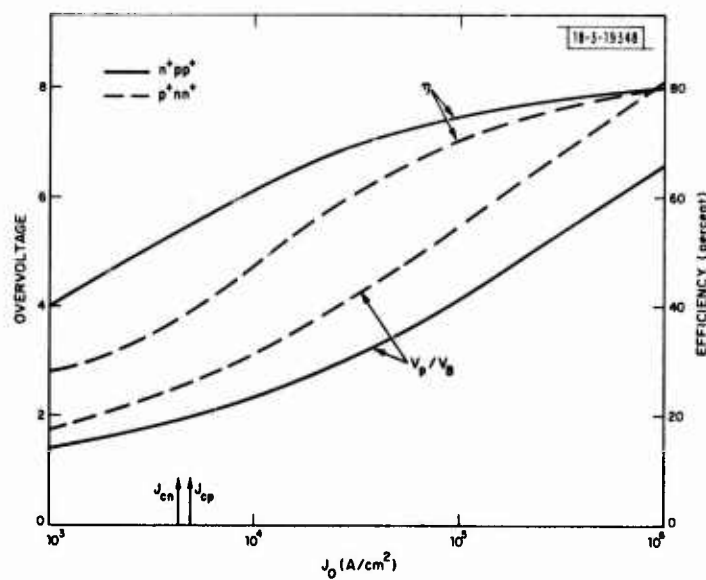


Fig. II-6. Dependence of efficiency and overvoltage on current density for n- and p-type diodes.

$t_c$  is the time needed to charge the diode by the current  $J_0$  from zero to  $V_B$  volts and is given by

$$t_c = \frac{\epsilon}{w} \frac{V_B}{J_0} \quad (\text{II-6})$$

The "on" time and "off" time are

$$t_{\text{on}} = t_d + t_p + t_c = t_{\text{off}} \quad (\text{II-7})$$

Once the waveforms have been determined, a Fourier analysis can be carried out to determine the power output and efficiency. Typical results are given in Figs. II-5 and -6. Figure II-5 shows that, for a given current density, the delay time  $t_d$  is smaller for the  $n^+pp^+$  structure and thus the required overvoltage is smaller. This results in an improved efficiency as can be seen in Fig. II-6. Figure II-6 also shows that the efficiency achievable in the  $n^+pp^+$  structure is greater, particularly at lower current densities where CW operation may be possible. A minimum current density given by  $J_c = qv_s N_d$  is usually required<sup>7,8</sup> to initiate an avalanche shock front and a trapped plasma. The minimum current densities for the n and p diodes,  $J_{cn}$  and  $J_{cp}$ , respectively, are indicated in Fig. II-6. Thus, it may be argued that these results are only applicable for values of  $J_0 > J_c$ . However, it was pointed out by Evans,<sup>17</sup> based on computer experiments, that the main features of the trapped plasma mode are retained even for values of  $J_0 < J_c$  (by a factor of 2 or more).

Fourier analysis of the current and voltage waveforms derived for each device also determines the impedance of the device at the fundamental and higher harmonics. Thus, this rather simple model can reveal some of the important operating characteristics and properties of the device, and the effects of various parameters upon its operation.

### C. HARMONIC EFFECTS

A detailed study of the effects of harmonics on efficiency and power output has been carried out by Trew,<sup>18</sup> using an approximate model for the device which incorporated several features not included in earlier approximate analyses.<sup>10</sup> This model permits arbitrary current waveforms which could be synthesized from a series of harmonics, and yielded current and voltage waveforms similar to experimentally observed ones.

Trew considered several realistic waveforms where the resulting impedances at all the harmonics have a negative real part. He also compared the results from his model with the experimental waveforms measured by Snapp<sup>19</sup> and found excellent agreement. He also showed that the operating properties of the device can be predicted quite accurately using only the first three harmonics.

The typical current and voltage waveforms presented above indicate that the efficiency and power output of a TRAPATT oscillator are highly dependent on the circuit. In particular, the circuit must present the proper impedance at the fundamental and also at harmonic frequencies. A typical example is shown in Fig. II-7 where the efficiency is plotted as a function of the 2nd-harmonic phase angle  $\phi_2$ . One sees that the efficiency at the fundamental frequency is highly affected by  $\phi_2$  as is the efficiency at the 2nd harmonic. Thus, the efficiencies at the fundamental and harmonic frequencies can be enhanced or reduced by circuit tuning. Because of this critical dependence on the impedance of the circuit at harmonic frequencies, it is difficult to tune an

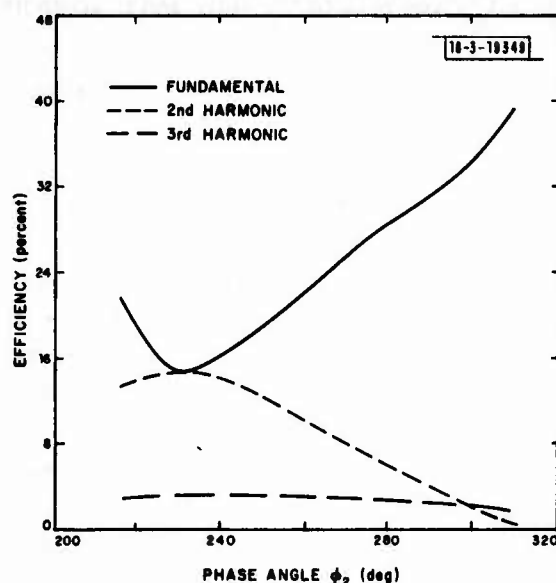


Fig. II-7. Relationship between efficiency and phase of 2nd-harmonic voltage.

oscillator continuously over a broad frequency range and maintain a constant power output and efficiency. This creates many problems in the broadbanding of TRAPATT amplifiers as will be discussed in Chaps. V and VI.

#### D. INITIATION OF THE TRAPATT MODE

The initiation of the TRAPATT mode is complex and not completely understood at this time. Several mechanisms are generally believed to be involved in the initiation of this mode of operation, and are discussed briefly here.

Many oscillators exhibit a small-signal negative conductance at the operating frequency. Thus, when such devices are placed in a proper circuit, oscillations will build up to a steady-state value which is determined by the circuit and the nonlinear behavior of the device. For stable oscillators, the negative conductance decreases with the amplitude of the oscillation and reaches a steady-state value equal to the circuit conductance.

TRAPATT oscillations are different in that the device does not always exhibit a small-signal negative conductance at the TRAPATT frequency, although in some instances one may exist. The initiation of the TRAPATT mode is believed to come about from a combination of the following interdependent factors:

- (1) Oscillations at the IMPATT frequency which start because of the inherent negative conductance of the device in the IMPATT frequency range;
- (2) The static DC I-V characteristic of the device which is highly dependent on the doping profile and the magnitude of the DC current. In many instances, the DC I-V characteristic exhibits a negative resistance which in turn can lead to bias-circuit oscillations or relaxation-type oscillators;
- (3) The dynamic DC I-V characteristic of a device, which is affected by the magnitude of RF oscillation at the IMPATT frequency;

- (4) Parametric-type interactions in the device which can result in a negative resistance at lower frequencies;
- (5) The rise time of the applied current pulse.

One or all these mechanisms in combination can lead to the overvoltage necessary to initiate the TRAPATT mode. Depending on the type of mechanism involved, the initiation time required will vary significantly. Finally, bias circuit design is important in TRAPATT circuits since some of these mechanisms can also contribute to diode burnout and spurious oscillations, or noise. All these mechanisms have been observed experimentally.<sup>20</sup>

The following discussion<sup>10</sup> is limited to  $p^+nn^+$  and  $n^+pp^+$  devices with uniform doping in the n and p layers, respectively, but can be extended to other structures.

- (1) The DC I-V characteristic in the absence of RF oscillation will exhibit a negative resistance at a certain critical current density, which depends on the doping in the n and p layer in a direct relationship. For example, the critical current density for a  $p^+-i-n^+$  structure is essentially zero.
- (2) For comparable doping levels, the critical current density for  $p^+nn^+$  devices is smaller than for  $n^+pp^+$  ones.
- (3) For both devices, the DC negative resistance increases with current density, beyond the critical value.
- (4) For both devices, the critical current density decreases as the amplitude of the RF oscillation at the IMPATT frequency increases.

Fig. II-8 demonstrates some of these effects.

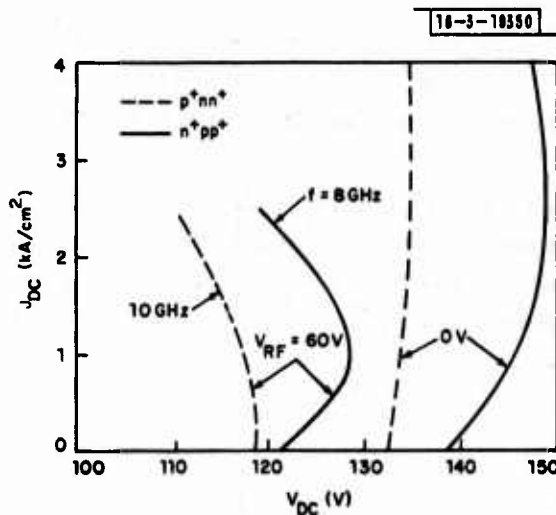


Fig. II-8. Dynamic current-voltage characteristics of p- and n-type diodes.

As a result, some of the ways the TRAPATT mode can be initiated are:

- (1) If the device I-V characteristic does not exhibit a DC negative resistance even in the presence of RF IMPATT oscillations, then the initiation mechanism will depend on IMPATT oscillations alone. In this case, the proper circuit impedance at the IMPATT frequency can cause the RF oscillations to build up to a large-enough amplitude to initiate the TRAPATT mode. Since p-type devices have a larger small-signal negative conductance than n-type ones, the starting current and the time for initiation of the TRAPATT mode will be lower for the former device.
- (2) Some devices do not exhibit a DC negative resistance in the absence of RF IMPATT oscillations. As the IMPATT oscillations build up, however, many devices will start exhibiting a DC negative resistance and will have a negative resistance over a wide range of low frequencies. This can then result in bias-circuit oscillations, or in relaxation-type oscillations which lead to the overvoltage required to initiate the TRAPATT mode. In this case, n- and p-type devices may be comparable. However, if the bias circuit is not properly designed, the n-type devices may be more susceptible to burnout and the power output and efficiency which may be achieved can be higher for p-type devices.<sup>18</sup>
- (3) If the device exhibits a DC negative resistance in the absence of RF oscillations, then the TRAPATT mode can be initiated from bias-circuit relaxation-type oscillations without requiring any IMPATT oscillations. In this case, the starting current and the time for initiation will be lower for the n-type device. Again, careful bias-circuit design is necessary to prevent burnout.
- (4) Another phenomenon which has been observed is related to the rise time of the bias-current pulse. If this rise time is very short, reflections in the circuit can lead to a high-enough voltage to initiate the TRAPATT mode.

All these effects also appear in TRAPATT amplifiers. However, since a large RF input signal is applied, this input signal itself can lead to initiation of the mode.

Some of the effects discussed above have been observed in a device-circuit interaction simulation program.<sup>20</sup> That work is continuing and may provide further insight into the operation of TRAPATT devices.

## CHAPTER III

### DEVICE DESIGN AND PRODUCTION

#### A. INTRODUCTION

There are a number of structures and methods currently in use for the fabrication of TRAPATT diodes, and this chapter is intended to review and compare the properties of the most important of these. It is not intended as a description of all the technological details which pertain to the production of devices.

TRAPATT oscillations have never been observed in GaAs, for reasons which are not presently understood. Thus, fabrication of these devices makes use of silicon technology, which is a relatively mature art. Differences between devices are largely those of: polarity (p- or n-type doping in the depletion region); type and depth of junction (deep or shallow diffused, shallow implanted, or surface Schottky barrier); direction of current flow [planar or vertical (mesa) orientation]; and cross-sectional classifications such as lumped or distributed area devices. Choices among these are driven by considerations of expected RF properties, available technology, passivation against surface effects, and thermal impedances. These will be discussed in detail in the following sections.

#### B. FABRICATION OF ETCHED-MESA DEVICES

The early history of the TRAPATT mode's discovery and investigation may be considered as an evolutionary perturbation on the broader development of solid-state microwave diodes. Thus, early fabrication techniques were very similar for both TRAPATT and IMPATT diodes, while the latter, in turn, closely resembled varactors and pin switching diodes. The etched-mesa structure has been commonly used for all of these. It is, therefore, important in a historical sense and is, as well, currently in use in a great number of these devices. It is also quite suitable for the tutorial purpose of illustrating the fabrication procedure.

The process begins with a wafer of low-resistivity semiconductor substrate upon which a thin layer has been grown (usually by either vapor or liquid-phase epitaxial growth techniques) with the proper doping concentration for the desired device. The substrate is then thinned by mechanical abrasion and/or chemical etching, in order to reduce series resistance in the completed device. After appropriate cleaning, surface resistivity measurements, and epitaxial thickness verification, a semiconductor junction is formed near the surface of the epitaxial layer. Diffusion or ion implantation of appropriate dopants might be used or, alternatively, Schottky barrier metallizations might be applied. After contact metallizations are in place on both sides of the wafer, photolithographic techniques are utilized to define the individual diodes, and the unwanted metal and semiconductor materials are removed from between the mesas by chemical etching.

Early attempts to increase the permissible current density in both TRAPATT and IMPATT diodes led to the so-called flip-chip structure, in which the completed mesa was bonded upside down in the package in an attempt to place the junction in close contact with the heat sink. While this resulted in improved power-handling capability, it was very difficult to obtain a good uniform thermal compression bond under the entire mesa because of surface nonuniformity, etc., and devices sometimes failed due to localized heating, and technology currently favors a mesa device with a heat sink plated integrally on the junction side of the device. This technique has



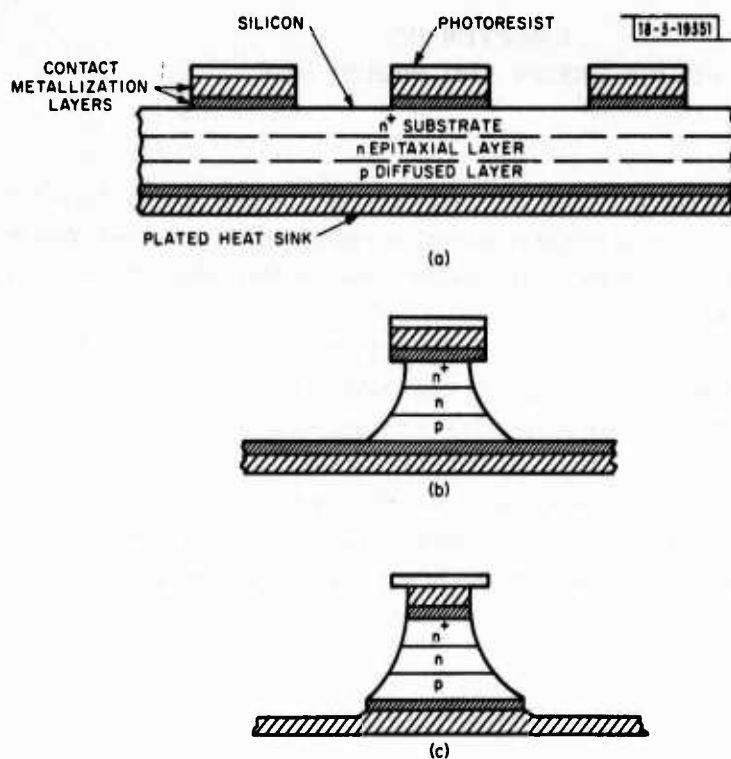


Fig. III-1. Fabrication of plated heat-sink mesa diodes: (a) wafer cross section after metallization etch, (b) mesa after etch, and (c) single device after separation etch.

the additional advantage that the heat sink is massive enough to permit easy handling of the separate diodes.

Figure III-1 illustrates several of these processing steps for the case of a diffused  $p^+nn^+$  silicon diode.

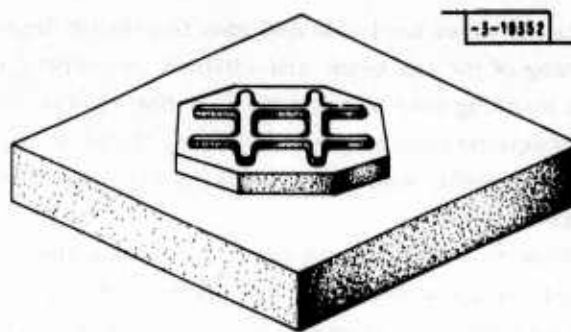
For pulsed TRAPATT devices, a so-called heat capacitor<sup>21</sup> consisting of a mass of copper soldered to the substrate side of the device has proven useful in extending the maximum pulse length before a given temperature rise occurs. The heat absorbed by the heat capacitor then flows out through the device during the "off" time between pulses.

There have been efforts to mount both IMPATT and TRAPATT devices on diamond heat sinks,<sup>22,23</sup> since type II-a diamond has a thermal conductivity about 3 to 5 times that of copper. This technique is unquestionably very effective in reducing the spreading component of the thermal resistance; but, to date, has not found widespread application most likely because of cost and added fabrication complexity.

### C. DISTRIBUTED AREA CROSS-SECTION DEVICES

The thermal resistance of large area diodes is dominated by the spreading resistance in the heat sink, so that attempts to increase the diodes' power-handling capability have led to cross-sectional shapes with large ratios of periphery to enclosed area. Stripes, annulus shapes, and arrays of separated smaller diodes are some of these. At RCA, a variation of the multiple-stripe diode called a cruciform structure combines several desirable properties such as a high ratio of periphery to enclosed area, a good geometry for uniformity of current distribution, and

Fig. III-2. Cruciform diode structure.



relative ease of bond-wire attachment. The long pulse, high power, high duty-cycle results obtained from these devices are reported in Chap. VI. Figure III-2 shows this cruciform structure.

Researchers at Sperry have favored the annular, or ring-shaped<sup>24</sup> structure mounted on a diamond heat spreader. Bond wires must be attached to this annulus at several spaces along the circumference to promote uniform current distribution, and the overall diameter must be limited to a value which will not permit moding, i.e., integer multiples of a half-wavelength at important operating harmonics of the output frequency. This includes at least the 2nd and 3rd, and possibly as high as the 5th harmonic.

Multiple parallel-connected, small circular diodes have been investigated at RCA, and dropped in favor of the cruciform structure, since it proved difficult to achieve reproducible, low-parasitic-capacitance interconnections without seriously compounding the difficulties associated with the fabrication technology.

Both the annular and cruciform structures have been made practical primarily by plated heat-sink technology. This provides a great deal of strength to support these high aspect devices in handling and packaging operations, and allows bonding or soldering to the package heat sink without voids or chip damage, which were frequently experienced with large devices prior to the advent of the integral plated heat sink.

#### D. JUNCTION FORMATION

The high electric fields necessary for the generation of carriers by impact ionization in the TRAPATT devices is provided by reverse biasing a semiconductor junction. This junction is usually formed between adjacent layers of semiconductor with respective doping concentrations of opposite polarity. In theory, the application of an appropriate metallization on either polarity of semiconductor, forming a Schottky barrier,<sup>25</sup> would provide a junction in close contact with the heat sink. In practice, such devices have not worked well, perhaps because of the soft breakdown characteristic of such a junction. The p-n junctions which have been used for TRAPATT diodes have been of the diffused, ion-implanted, or epitaxially grown types.

Diffused junctions are made by holding the wafer at an elevated temperature for a controlled length of time in the presence of an appropriate impurity diffusant. The impurity source may be gaseous mixture introduced into the diffusion furnace or a liquid coating on the wafer.

Implanted junctions are produced by accelerating a beam of ionized particles to high kinetic energy levels and allowing them to impinge upon the wafer surface. Close control of the quantity of implanted charge is maintained by monitoring the ion current, while depth of the implant is controlled by the beam potential. Following the implantation, the ions are electrically activated and lattice damage is repaired by annealing the wafer. High annealing temperatures may



be used to drive the implanted ions to greater depths by diffusion, if desired. Focusing and scanning of the ion beam are utilized to achieve uniformity in the implanted cross section, while masking may be provided to define cross-sectional areas to be implanted.

Junctions may be grown by either liquid or vapor phase epitaxy, with very precise control of doping profile achieved by varying the composition, flow rates, and temperatures of the reactants.

Finally, junctions are characterized as abrupt or graded depending upon the nature of the spatial change in impurity concentration across the junction. When the concentration is constant on each side, changing abruptly from donor to acceptor at the junction, one has the so-called "abrupt junction." If the impurity concentration is much higher on one side than the other, it is a "one-sided abrupt junction," and the electric field under reverse bias will be contained almost entirely in the lightly doped side. If, instead, the impurity concentration varies smoothly with distance across the junction, one has the so-called graded junction, with the linear-graded junction as a special case. Figure III-3 shows the doping concentration and built-in electric field profiles for abrupt and linearly graded junctions.

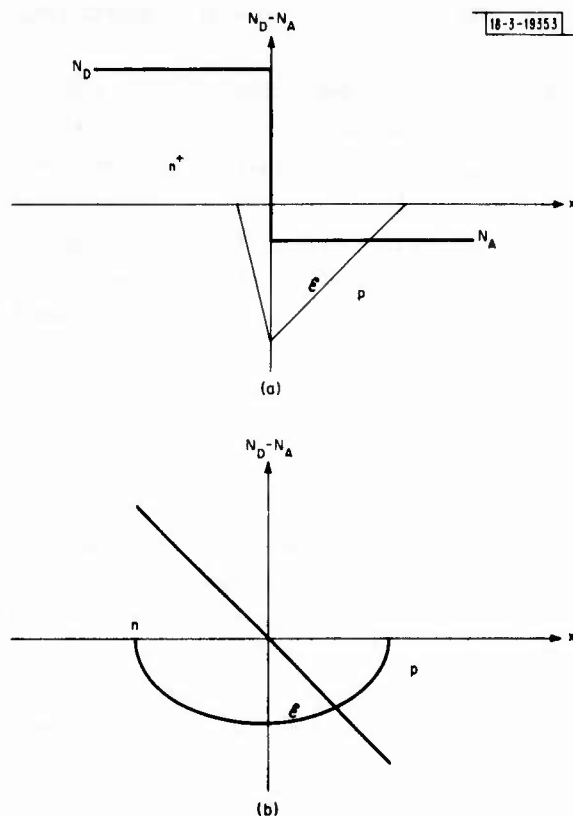


Fig. III-3. Profiles of (a) one-sided abrupt and (b) linearly graded junctions.

Shallow diffused junctions are approximated by abrupt junctions, while deep diffused junctions tend to be graded. Implanted and epitaxially grown junctions may be controlled to approximate either type.

The RF performance obtained from TRAPATT diodes tends to favor the graded junction, since they appear to be less susceptible to burnout at low current levels. RCA claims a wider optimum depletion region for a fixed frequency,<sup>26</sup> although they have not shown this conclusively by either theory or experiment. A wider depletion region is desirable since it raises the

impedance level of a fixed area device, thereby permitting higher power and broader bandwidth operation.

Finally, graded junctions located near the surface of the wafer (that is, adjacent to the heat sink) are desirable for their improved thermal properties. These can be achieved by ion implantation or epitaxial growth techniques.

#### E. PLANAR-TYPE DEVICES

Surface instabilities have been suspected by several researchers<sup>27-29</sup> as a cause of performance degradation in TRAPATT oscillators and amplifiers. Various techniques for passivation of the exposed junction edge around the circumference of a mesa device have been tried, are usually considered proprietary, and have produced varying degrees of success. One of the more interesting approaches to junction passivation is the use of planar technology, in which the junction is formed by diffusion through a window in a masking passivant, such as silicon dioxide. Since the diffusant tends to spread both sideways and downward through the window, the actual junction edge position will be located under the diffusion mask. Figure III-4(a) shows an example of a planar TRAPATT diode cross section.

A variation of the planar technique developed at Sperry<sup>30</sup> is shown in Fig. III-4(b). Here the active portion of the junction is contained within the bulk of the semiconductor material.

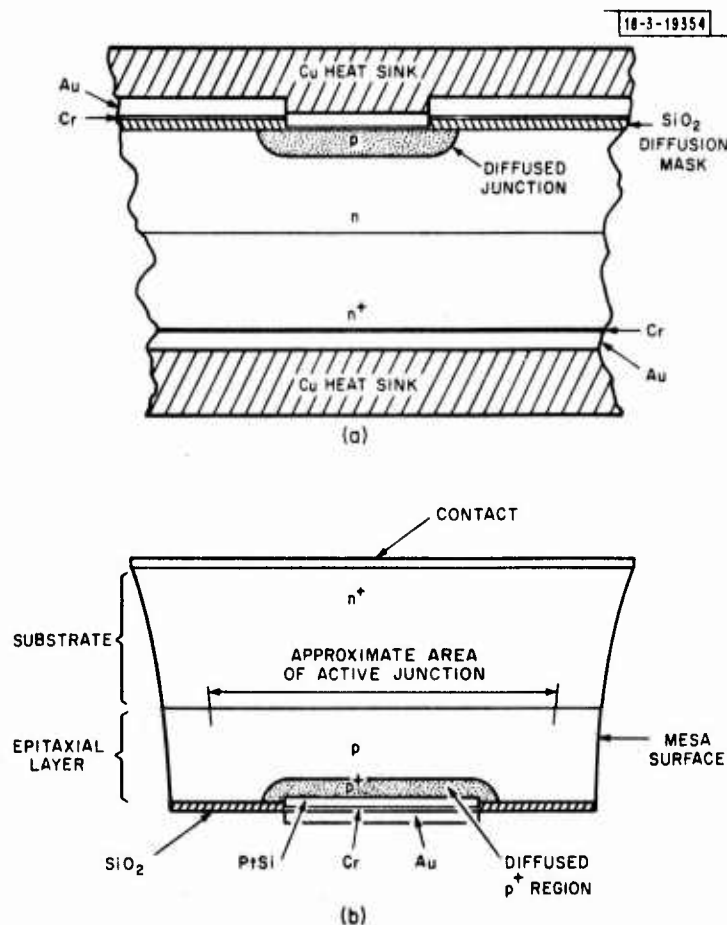


Fig. III-4. Cross-section views of planar-type devices: (a) planar diode and (b) inactive surface mesa diode.

RF performance of as high as 500 W of oscillator power at 1.4 GHz with 30-percent efficiency has been claimed from an array of seven planar diodes at RCA, for 0.5- to 1.0- $\mu$ sec pulse lengths at 2-percent duty. The only performance data given for the Sperry diodes indicate an efficiency improvement but reduced power-handling capability, when compared to conventional mesa diodes.

## CHAPTER IV STATE OF THE ART

### A. TRAPATT OSCILLATORS

Table IV-1 indicates the current state of the art for power generation and efficiency for TRAPATT oscillators. The information is arranged by date of the reporting reference, and is provided for both CW and pulsed operation. For convenience, references are listed in Tables IV-1 and -2 using an alphabetic citation scheme to avoid confusion with the complete list of references from the remainder of this report. Figure IV-1 illustrates these results on a power-frequency basis.

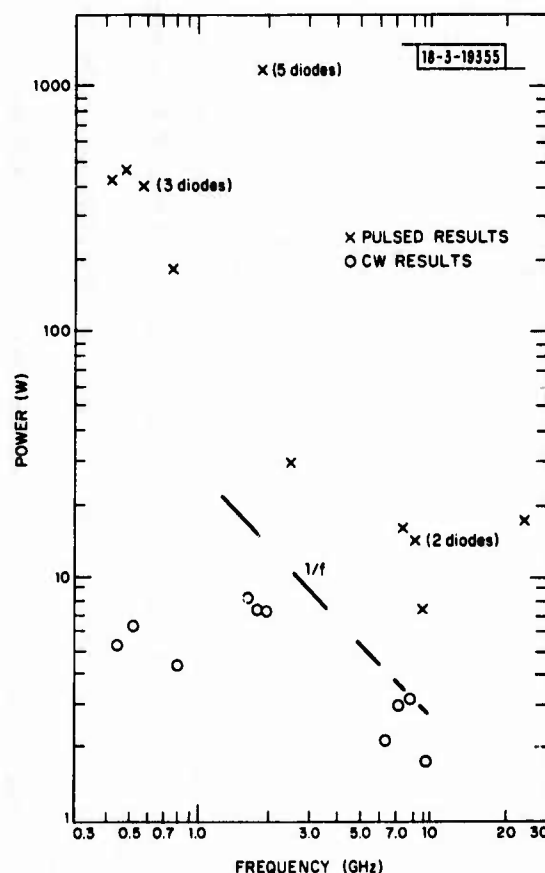


Fig. IV-1. TRAPATT oscillator power-frequency state of the art.

### B. TRAPATT AMPLIFIERS

Table IV-2 indicates the output power, gain, bandwidth, efficiency, pulse width, and duty cycle of representative state-of-the-art TRAPATT amplifiers. As above, the data are presented in chronological order, and the alphabetic reference scheme is preserved. All the tabulated results are for pulsed operation. The bandwidth is given for a 1-dB-output power variation.

TABLE IV-1  
TRAPATT OSCILLATOR STATE OF THE ART

Part A - CW Results

Number of Diodes	Type of Diode	Type of Circuit	Frequency (GHz)	Power Output (W)	Efficiency (percent)	Reference
1	<sup>+</sup> p-n-n	coaxial	0.45	5.3	43	a
1	<sup>+</sup> p-n-n	coaxial	0.52	6.4	26.2	b
1	<sup>+</sup> n-p-p	coaxial	0.8	4.5	39	c
1	<sup>+</sup> p-n-n	coaxial	8.0	3.3	18.5	d
1	<sup>+</sup> p-n-n	coaxial	9.8	1.8	10.5	d
1	<sup>+</sup> n-p-p	coaxial	7.2	3.0	14.0	e
1	<sup>+</sup> n-p-p	coaxial	1.62	8.3	22	f
1	<sup>+</sup> n-p-p	coaxial	1.80	7.5	20	f
1	<sup>+</sup> n-p-p	coaxial	1.91	7.3	24	f
1	<sup>+</sup> n-p-p	coaxial	2.13	6.4	16	f

- a. D.E. Iglesias and W.J. Evans, "High-Efficiency CW IMPATT Operation," Proc. IEEE (Correspondence) 56, No. 9, 160 (September 1968).
- b. W.J. Evans and D.E. Iglesias, "CW Silicon TRAPATT Operation," Proc. IEEE (Letters) 58, No. 2, 285-286 (February 1970).
- c. R.W. Bierig, R.F. Bera, and M.R. Harris, "Complementary TRAPATT Diode Oscillators," IEEE Int. Solid-State Circuits Conference, Philadelphia, February 1972, pp.200-201.
- d. N.W. Cox and K.E. Gsteiger, "X-Band CW TRAPATT Oscillators Using Ring Diodes on Diamond Heat Spreaders," Electron. Lett. 9, No. 12, 269-270 (June 1973).
- e. T.T. Fong and R.S. Ying, "Complementary X-Band TRAPATT Diodes," 1974 IEEE S-MTT Int. Microwave Symposium Digest of Technical Papers (IEEE, New York, 1974), pp.365-366.
- f. K.R. Gleason, E.D. Cohen, and M. L. Bark, "TRAPATT Devices for High Power, Long Pulse, and CW Applications," Government Microcircuits Applications Conference, Lake Buena Vista, Florida, November 1976.

TABLE IV-1 (Continued)

Part B - Pulsed Results									
Number of Diodes	Type of Diode	Type of Circuit	Frequency (GHz)	Power Output (W)		Pulse Width (μsec)	PRF (Hz)	Efficiency (percent)	Reference
				Peak	Average				
1	<sup>+</sup> p-n-n <sup>+</sup>	coaxial	0.425	435				25	g
1	<sup>+</sup> p-n-n <sup>+</sup>	coaxial	0.775	180				60	g
1	<sup>+</sup> p-n-n <sup>+</sup>	distributed	24	17	0.007	0.4	1,000	24	h
3	<sup>+</sup> p-n-n <sup>+</sup>	coaxial and microstrip	0.57	395	0.2	0.5	1,000	75	i
1	<sup>+</sup> p-n-n <sup>+</sup>	coaxial	7.5	16	0.03	0.2	10,000	43	i
5	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	1.9	1,200	1.0	0.5-1.0	1,000	24	k
1	<sup>+</sup> p-n-n <sup>+</sup>	lumped	0.5	470	4.7	0.2	50,000	44	l
2	<sup>+</sup> n-p-p <sup>+</sup>		8.36	14.3		0.2		16.5	m
1	<sup>+</sup> n-p-p <sup>+</sup>	coaxial	2.5	30	0.3	100	10	30	n
1	<sup>+</sup> p-n-n <sup>+</sup>	coaxial	9.2	7.4	0.04	0.4	12,500	30.6	o

g. K. K. N. Chang, "Avalanche Diodes as UHF and L-Band Sources," RCA Rev. (Radio Corp. Am.) 30, No. 1, 3-14 (March 1969).

h. S. G. Liu, J. J. Risko, and K. K. N. Chang, "High-Power K-Band Silicon Avalanche-Diode Oscillators," Proc. IEEE (Letters) 58, No. 6, 919-920 (June 1970).

i. D. F. Kostishack, "UHF Avalanche Diode Oscillator Providing 400 Watts Peak Power and 75 Percent Efficiency," Proc. IEEE (Letters) 58, No. 8, 1282-1283 (August 1970).

j. M. I. Grace, H. Kroger, and J. Telio, "Improved Performance of X-Band TRAPATTs," Proc. IEEE (Letters) 60, No. 11, 1443-1444 (November 1972).

k. S. G. Liu, "2000 W GHz Complementary TRAPATT Diodes," 1972 IEEE Int. Solid-State Circuits Conference Digest of Technical Papers (IEEE, New York, 1972), pp. 124-125.

l. A. S. Clorfeine, H. J. Proger, and R. D. Hughes, "Lumped-Element High-Power TRAPATT Circuits," RCA Rev. (Radio Corp. Am.) 34, 581-595 (December 1973).

m. K. R. Gleason, C. T. Rucker, N. W. Cox, A. C. Macpherson, and E. D. Cohen, "Experimental Study of Series Connected TRAPATT Diodes," IEEE Trans. Microwave Theory Tech. MTT-22, No. 8, 804-806 (August 1974).

n. H. Kroger and M. I. Grace, "TRAPATT Amplifier," Final Report RADC-TR-74-261, Sperry Rand Research Center (January 1975).

o. J. J. Purcell, "High-Efficiency TRAPATT Operation in X-Band," Electron. Lett. 11, No. 11, 236-237 (May 1975).

Number of Diodes	Type of Diode	Type of Circuit	Frequency (GHz)	Power Output (W)	Gain (dB)	Bandwidth (MHz)	Efficiency (percent)	Pulse Width (μsec)	Duty Cycle (percent)	Reference
1	<sup>+</sup> p-n-n <sup>+</sup>	microstrip	3	50	10	50	14	10	5.6	p
1	<sup>+</sup> p-n-n <sup>+</sup>	microstrip	3.27	200	13	narrow	not given			q
1	<sup>+</sup> n-n-p-p <sup>+</sup>	microstrip	3	157	8.7	150	-	1.0	0.01	r
1		coaxial	3.15		7.5	300	20			s
19	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	3.05	130	6.5	350	14.2	5	0.02	t
1	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	3	50	3	narrow	5.0	100	4.2	u
1	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	3	68	5	narrow	9.0	50	5.0	u
1	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	3.1	125	9	400	23	0.2	0.1	v
2	<sup>+</sup> n-p-p <sup>+</sup>	microstrip	3.1	290	5.5	360	22	0.2	0.1	v
1	<sup>+</sup> p-n-n <sup>+</sup>	lumped element	3.3	50	6.0	250	17	1.0	0.1	w

p. K.K.N. Chang, H.J. Kawamoto, H.J. Prager, J. Reynolds, A. Rosen, and V.A. Milkinas, "High Efficiency Avalanche Diodes (TRAPATT) for Phased-Array Radar Systems," 1973 IEEE Int. Solid-State Circuits Conference Digest, pp. 122-123.

q. H. Kawamoto and H.J. Prager, "S-Band Avalanche Diode Amplifiers," Final Report, prepared by RCA Laboratories, Princeton, for M.I.T. Lincoln Laboratory (October 1973).

r. H. Kawamoto, S.G. Liu, H.J. Prager, and E.L. Allen, Jr., "S-Band TRAPATT Amplifiers with Four-Layer Diode Structures," RCA Rev. (Radio Corp. Am.) 35, No. 3, 372-386 (September 1974).

s. H. Kroger and M.I. Grace, "TRAPATT Amplifier," Final Report RADC-TR-74-261, Sperry Rand Research Center (January 1975).

t. A. Rosen, H. Kawamoto, J. Klatskin, and E.L. Allen, Jr., "Integrated TRAPATT Diode Arrays," IEEE Trans. Microwave Theory Tech. (Short Paper) MTT-23, No. 10, 841-843 (October 1975).

u. A. Rosen, P.T. Ho, and J.B. Klatskin, Final Report ECOM-74-0180-2, RCA Laboratories (February 1976).

v. T.T. Fong et al., "F-Band TRAPATT Amplifier," Final Report, Contract No. N0039-75-C-0081, Torrance Research Center, Hughes Aircraft Company (March 1976).

w. G.B. Jones and R.W. Laton, "Power Gain and Phase Performance of S-Band TRAPATT Amplifiers," Government Microcircuits Applications Conference, Lake Buena Vista, Florida, November 1976.



## CHAPTER V

### AMPLIFIER DESIGN PRINCIPLES

#### A. INTRODUCTION

The wideband TRAPATT amplifier is a two-terminal, large-signal, negative-resistance, circulator-coupled amplifier. The negative resistance is induced by the application of an external sinusoidal signal whose amplitude exceeds a critical value. The magnitude of the negative resistance depends upon the TRAPATT semiconductor parameters, bias conditions, and the external circuit. The amplifier behaves as a saturated amplifier, having a small dynamic range, low gain and high DC-to-RF conversion efficiency. The microwave characteristics of the TRAPATT amplifier have stimulated interest in its use as a final-stage amplifier for a phased-array radar.

The operation of the basic TRAPATT oscillator, which depends upon the phenomenon of "time-delayed-triggering," as described by Evans<sup>17</sup> is reviewed in Sec. B. The reasons for such circuits' lack of suitability for broadband amplifiers are described and their design principles are contrasted with the requirements for a true broadband amplifier. Section C presents a theoretical procedure, based on Carroll's description of TRAPATT oscillators<sup>31</sup> which permits the design and synthesis of microwave circuits which will permit broadband TRAPATT amplification. The circuit realization techniques developed for broadbanding TRAPATT amplifiers are described in Sec. D. The unsolved problems associated with the operation of amplifiers, including those which operate at harmonics of the fundamental frequency are discussed in Sec. E.

#### B. TRAPATT OSCILLATORS AND AMPLIFIERS

Time-Delayed-Triggered Mode (Evans Circuit):— Realization of broadband TRAPATT amplifiers requires special device and circuit characteristics which differ from those of conventional TRAPATT oscillators and amplifiers. The majority of results reported for such oscillators and amplifiers have been obtained with circuits which utilize time-delayed triggering (TDT) as the oscillation-sustaining mechanism. A description has been published by Evans *et al.*<sup>17,32</sup> A fundamental characteristic of all TDT circuits is the requirement for a low-pass or bandpass filter at an appropriate location between the semiconductor device and the output load. A schematic diagram of the equivalent microwave circuit for a TDT TRAPATT amplifier is shown in Fig. V-1. The semiconductor device is connected to an output load resistor through a network comprising the parasitic elements of the diode package, a low-pass filter, and an impedance-matching network. The low-pass filter is located at an electrical distance  $\theta = (\lambda_0/2 - \delta)$ , where  $\delta$  is small compared to  $\lambda_0/2$ , from the TRAPATT device. The wavelength  $\lambda_0$  corresponds to a frequency  $\omega_0$  defined as the normal-mode frequency for the TDT circuit. An impedance-matching network, located between the low-pass filter and the output load, is used to adjust the circuit for optimum performance (either as an amplifier or oscillator).

The operation of a TDT circuit may be described with the help of Fig. V-1. If a sufficiently large transient overvoltage is applied across the TRAPATT diode, a traveling avalanche shock front (ASF) is initiated.<sup>31</sup> During the time this zone travels across the depletion region, the diode voltage drops and the diode current increases. When the ASF has completely traversed the depletion width, the instantaneous diode voltage drops to nearly zero. Thus, a voltage step, whose magnitude is on the order of the diode breakdown voltage, is generated. This step then



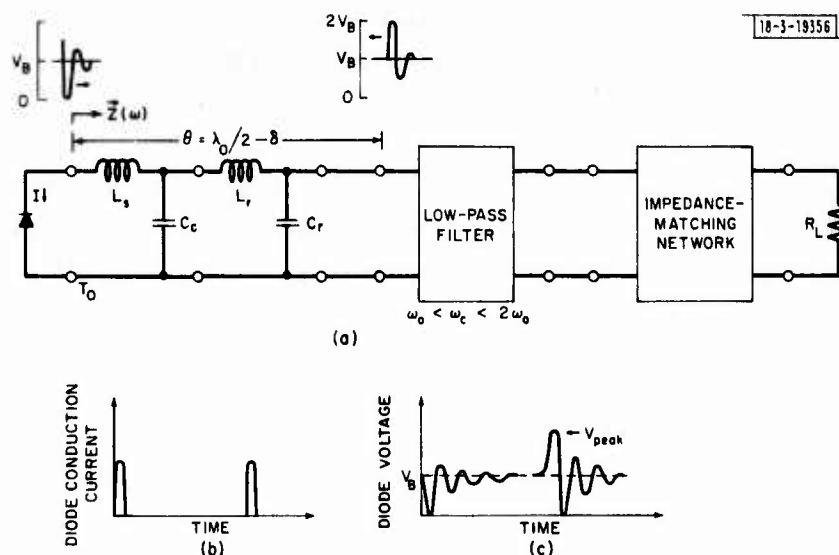


Fig. V-1. TDT TRAPATT oscillators: (a) simplified circuit model, (b) diode conduction current vs time, and (c) diode voltage vs time.

propagates through the parasitic reactances and along the section of uniform transmission line to the filter, whose high-frequency impedance is nearly a short circuit. The amplitude of the reflected pulse is only slightly less than the amplitude of the incident pulse, but is, however, of opposite sign. The reflected pulse arrives back at the diode with a total time delay corresponding to one period of the normal-mode frequency  $\omega_0$ . The diode voltage at that instant is thus driven to approximately twice the diode breakdown voltage, a new ASF is triggered, and the entire process repeats itself. Hence, the mechanism is self-sustaining. The strong dependence of the triggering mechanism on the circuit serves to emphasize the overall interdependence of TRAPATT circuits and devices.

A TRAPATT oscillator is operated as an amplifier using an externally applied AC signal to initiate the ASF (Ref. 33). In the externally excited mode, each RF cycle must be triggered only by the input signal. As might be expected, external excitation of the TRAPATT mode is most easily observed when the frequency of the applied signal is close to  $\omega_0$ , the normal-mode frequency of the TDT circuit. When the applied-signal frequency  $\omega_s$  is equal to the normal-mode frequency  $\omega_0$ , the TDT enhances the triggering of an ASF. When  $\omega_s$  is different from  $\omega_0$ , multiple signal frequencies are observed at the output. In general, the two most important frequencies are the applied-signal frequency  $\omega_s$  and the normal-mode frequency  $\omega_0$ , but difference frequencies can be observed as well. Observation of the normal-mode frequency as well as the applied signal at the output port can be explained by the normal TDT mechanism. That is, when the applied-signal voltage triggers an ASF, the diode voltage drops toward zero and reverses rapidly. Thus, a narrow voltage pulse, whose magnitude is on the order of the breakdown voltage, is generated and propagates down the transmission line (as illustrated in Fig. V-1). At distance  $\theta \approx \lambda_0/2$ , the pulse is reflected from the filter, as before, with near unity magnitude, but changed in sign. The reflected pulse then arrives back at the diode with a total time delay of  $2\pi/\omega = \lambda_0/c$  and instantly drives the voltage at the diode to about twice the diode breakdown voltage, triggering an ASF within the diode. This sequence is just the usual TDT mode as described above, and the frequency of this overvoltage corresponds to the normal mode of TDT frequency  $\omega_0$ . In general, TDT circuit amplifiers have relatively narrow useful

bandwidths (on the order of 2 percent) due to this spurious signal generation, but may be operated in a Class C mode where large bias current flows only when an RF input signal is applied.<sup>34</sup>

Not all TRAPATT amplifier circuits must necessarily function in this TDT manner. The diode terminal voltage generated in response to the impulsive diode conduction current incident at terminal reference plane  $T_0$  can be adjusted to be self-consistent with TRAPATT theory through the proper choice of the terminal load impedance  $Z(\omega)$ . The TDT network described by Evans is only one of many such circuits that is self-consistent with a theoretical TRAPATT current and voltage waveform. The broadband operation of TRAPATT circuits will necessitate the synthesis of such circuits which neither depend upon nor permit a narrowband triggering mechanism.

### C. CARROLL THEORY FOR TRAPATT AMPLIFIERS

#### 1. Introduction

A simplified theory for the device-circuit interaction for Evans-type TRAPATT oscillators was developed by Carroll<sup>34</sup> and later extended by Carroll and Crede<sup>35</sup> to include the effects of the microwave circuit parameters on TRAPATT performance.

The Carroll theory is based upon the important insight that the interaction between a TRAPATT diode and the associated microwave circuit in which the diode is embedded can be approximated by a simple model. When the voltage across the depletion layer of a TRAPATT diode and its time derivative exceed certain critical values, the device acts as an impulsive particle current generator in shunt with the electronic reactance and the depletion layer capacitance.

This basic model for the TRAPATT circuit and diode is shown in Fig. V-2. The diode is represented by a particle current generator in shunt with the depletion layer capacitance  $C_0$ . The quantities  $L_a$ ,  $L_s$ ,  $C_c$ ,  $L_r$ , and  $C_r$  represent the electronic reactance, parasitic lead inductance, case capacitance, and a radial line transformation from the diode package to the TEM mode in the circuit. An ideal low-pass filter is located a distance  $l$  from the diode package. It is assumed that the low-pass filter passes the fundamental operating frequency unattenuated and is a short circuit to all harmonics of the fundamental frequency.

The current generator  $H$  injects an impulsive current density that is induced by the charge carriers generated by the avalanche multiplication. This is a particularly useful model because the device physics of the ASF indicate that the induced current has a large impulsive component which controls the voltage response of the circuit. The shape of the particle current  $H$  is assumed to be that of a short pulse, as shown in Fig. V-2; whereas the total current through the diode  $J$  is assumed to have a rectangular form that is consistent with Clorfeine's device theory.<sup>8</sup> These assumptions regarding  $J$  and  $H$  also determine the time-varying part of the voltage  $V$ , since

$$J = H + C_0 \frac{dV}{dt} + \frac{1}{L_a} \int V dt \quad (V-1)$$

It can be seen from Fig. V-2 that the voltage across the diode is self-consistent with the TRAPATT mode theory (e.g., there is a large overvoltage that can trigger an ASF, causing the diode voltage to drop to zero and then recover).

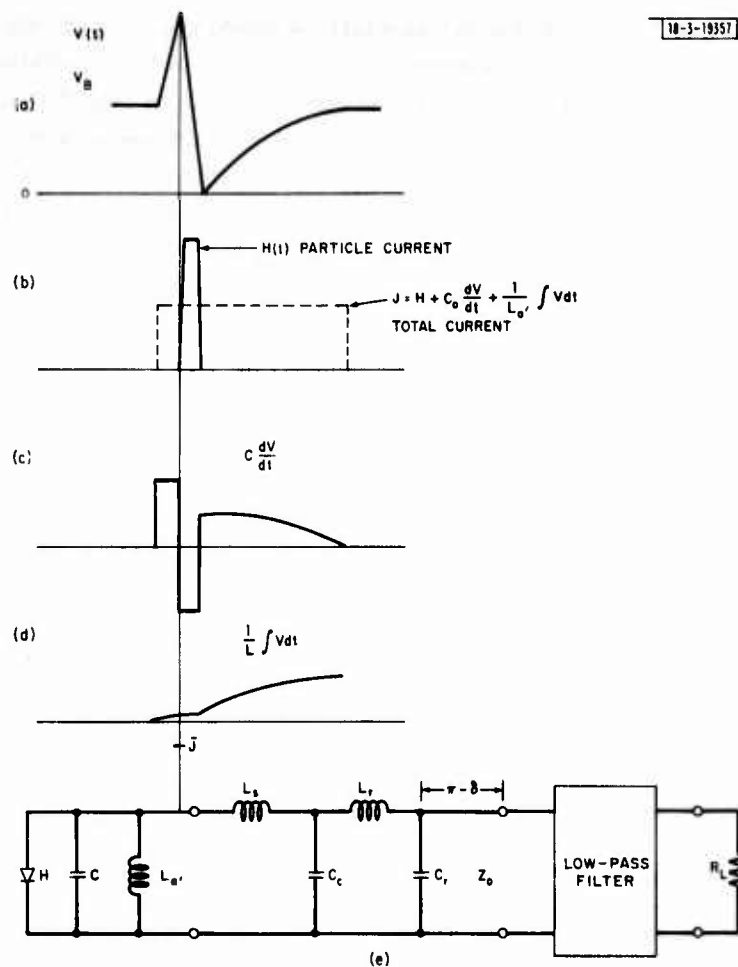


Fig. V-2(a-e). TRAPATT diode voltage-current components.

The circuit used for the TRAPATT amplifier is different from that of the TRAPATT oscillator in that the steady-state response of the amplifier circuit should exhibit a voltage waveform that does not have a sufficient "overvoltage" to trigger an ASI unless an external voltage at the operating frequency is applied.

If we assume that the diode particle current  $H$  can be represented by a recurrent delta function with repetition period  $T$ , then

$$H(t) = Q \text{ Rep}_T \delta(t) \quad 0 \leq t \leq \infty \quad (V-2)$$

where  $I_0 = Q/T$  is the average value of the particle current. The steady-state voltage across the diode determined by Carroll<sup>8</sup> making use of pseudotransients is given by

$$V_0 = V_{DC} + V_0 \frac{\sinh p(\theta - \pi)}{\sinh p\pi} - V_1 \cos(\theta - \phi) \quad (V-3)$$

where  $V(\theta + 2\pi) = V(\theta)$ ,  $\theta = \omega_0 t$ ,  $\omega_0 = 2\pi/T$ ,  $\phi$  represents the phase of the power extraction portion of the waveform voltage, and  $p (\approx 1/\omega_0 C_j Z_0 \delta)$  is a parameter which describes the time rate of change of voltage.

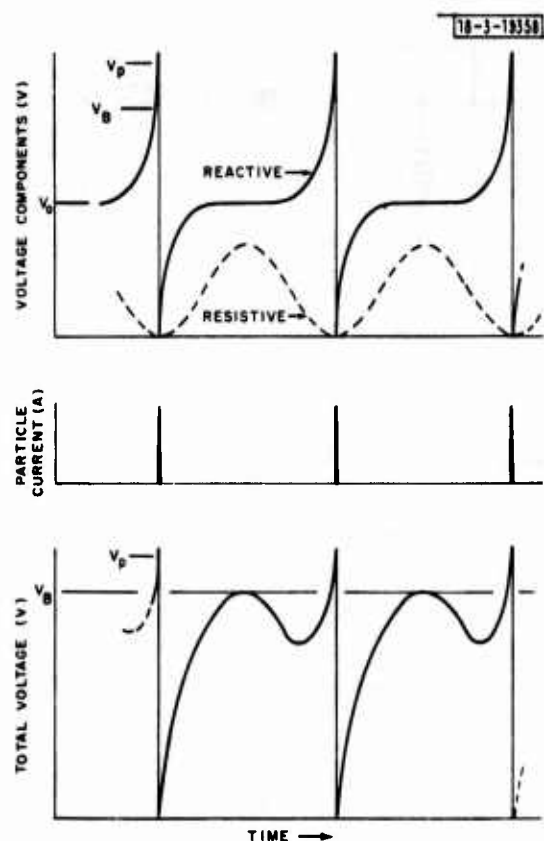


Fig. V-3. TRAPATT circuit voltage waveforms.

The elements of TRAPATT operation can be seen by examining this voltage waveform, as shown in Fig. V-3. As the diode fires (ASF excited), an impulse of particle current collapses the reactive component of voltage from  $V_p$  to nearly zero, and it then grows exponentially as a sinh function. The power extraction is modeled by adding an additional resistive voltage component which is in antiphase with the current pulse, as shown schematically in Fig. V-3. The maximum fundamental voltage swing is determined by the condition that premature avalanche should not occur, i.e., the total voltage must not exceed  $V_b$  prior to the reactive triggering of the ASF. The reactive termination at the harmonic serves the function of pretriggering the TRAPATT mode, while the resistive impedance that is added across the diode at the fundamental extracts the power through the low-pass filter with a minimum alteration of the triggering process. In order to trigger the ASF, the voltage must rise fast enough so that  $C_o \partial V / \partial t$  exceeds critical current at breakdown. This current,  $I_{crit}$ , is given by  $I_{crit} = q N_D v_s A$ , where  $q$  is the electronic charge,  $v_s$  is the high-field-saturated drift velocity,  $N_D$  is the ionized donor density, and  $A$  is the cross-sectional area of the device. On this basis, if  $p$  is too small, the rate of rise of voltage will fail to initiate an ASF. It should be noted that the charge  $Q$  must be sufficient to make the circuit voltage fall to zero if the low-impedance plasma state of the diode is to be matched.

## 2. Admittance Characteristics for TRAPATT Amplifiers

From the Carroll analysis<sup>35</sup> of Sec. C-1, we have shown that a self-consistent TRAPATT voltage and current waveform can be represented by the sum of a DC voltage component, a

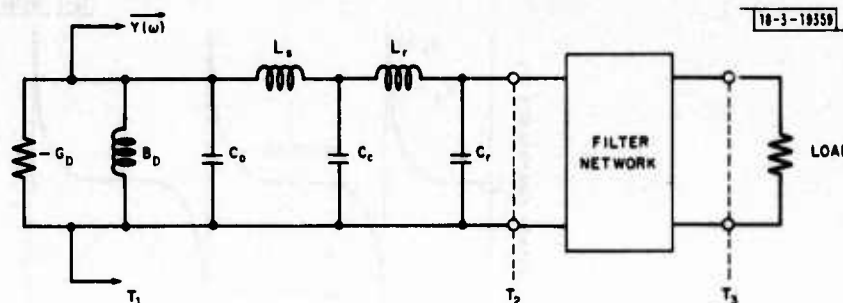


Fig. V-4. Large-signal equivalent circuit for wideband TRAPATT amplifier.

reactive voltage component, and a power-extraction voltage component. Assuming that the reactive voltage-triggering waveform can be generalized for all TRAPATTs, then an equivalent harmonic driving point admittance, whose properties are such that the terminal voltage response due to a periodic impulse current is self-consistent with the TRAPATT theory, can be postulated. The circuit model used for determining the harmonic driving point admittance is shown in Fig. V-4. The terminal current and voltage as a function of time were given by Eqs. (V-1) and (V-3), respectively. The reactive voltage-triggering waveform, generalized for all TRAPATT devices, is given by Eq. (V-4).

$$V_{\text{trig}} = V_o \frac{\sinh p(\theta - \pi)}{\sinh p\pi} \quad (\text{V-4})$$

where  $0 < p < 1$ ,  $\theta = \omega_o t$ ,  $0 < \theta < 2\pi$ . The triggering waveform is reactive in that the power dissipated per cycle is

$$\text{Power} = \frac{1}{T} \int_0^T V_{\text{trig}} \cdot H(t) dt = 0 \quad (\text{V-5})$$

The Fourier expansion of the reactive voltage is

$$V(t) = \frac{-4V_o}{\pi} \sum_{n=1}^{\infty} \frac{n}{p^2 + n^2} \text{Re}\{\exp[j(n\omega_o t - \pi/2)]\} \quad (\text{V-6})$$

The Fourier expansion for impulse current  $H(t)$  is given by

$$H(t) = i(t) = -2 \frac{Q}{T} \sum_{n=1}^{\infty} \text{Re} e^{jn\omega_o t} \quad (\text{V-7})$$

The harmonic driving point admittance [ratio of  $I(n\omega_o)$  to  $V(n\omega_o)$ ] is

$$\vec{Y}(n\omega_o) = jY_o \frac{p^2 + n^2}{2n\pi} \quad (\text{V-8})$$

where  $Y_o = I_o/V_o$ , and  $I_o = Q/T$ . The  $Y(n\omega_o)$  at the harmonic frequencies is thus specified for the self-consistent TRAPATT triggering.

Carroll<sup>31</sup> has shown that the low-pass filter circuit described by Evans will present an admittance  $Y(n\omega_o)$  which satisfies these harmonic admittance requirements over at least a decade in frequency. However, the time-delay triggering associated with the Evans-type circuit has limited such amplifiers to narrow bandwidths.

## D. WIDEBAND AMPLIFIER CIRCUITS

### 1. General Circuit Conditions

Investigations of TDT amplifiers and oscillators have defined certain circuit and device parameters necessary for achieving broadband TRAPATT amplification. The circuit model developed for broadband amplification is shown in Fig. V-4. The TRAPATT device is represented by a parallel circuit comprising a conductance  $G_D$ , an electronic susceptance  $B_D$  (which represents the active portion of the diode), and a capacitance  $C_O$  representing the depletion layer capacitance at breakdown. The inductance  $L_S$  and capacitance  $C_C$  represent parasitic lead inductance and standoff or package capacitance. The inductance  $L_T$  and capacitance  $C_T$  represent discontinuity reactances due to the connection of the diode mount to the microwave circuit.

The filter network defined at reference terminal planes  $T_2$ - $T_3$  forms the microwave impedance-matching network that performs the necessary fundamental and harmonic impedance matching for the TRAPATT device.

The terminal voltage-current characteristics and bandpass performance of the TRAPATT amplifiers can be predicted from the input admittance  $Y(\omega)$  at terminal reference plane  $T_1$  and the transfer characteristics  $H(\omega)$  of the impedance-matching network formed by the network elements between terminal reference planes  $T_1$  and  $T_3$ .

The power gain of the amplifier is given by the square of the magnitude of the reflection coefficient  $|\Gamma|^2$  at reference plane  $T_1$ , i.e.,

$$\text{Power Gain} = |\Gamma|^2 = \left| \frac{\bar{Y}(\omega) - G_D(\omega)}{Y(\omega) + G_D(\omega)} \right|^2 \quad (\text{V-9})$$

where  $G_D$  is the large signal conductance of the TRAPATT device and is negative at the fundamental and harmonic frequencies.

Broadband efficient amplification is obtained when the microwave impedance-matching filter fulfills the following conditions:

(a) Grace<sup>33</sup> has identified five device-circuit interaction conditions:

- |   |  |
|---|--|
| (1) $\text{Im } Y(\omega_0) = 0$  | Network is resonant at the output frequency.   |
| (2) $\text{Re } Y(\omega_0) = -KG_D$                                    | The factor $K$ is chosen for the desired gain.   |
| (3) $\text{Re } Y(n\omega_0) \approx 0, n > 1$                          | To minimize real power dissipation at harmonics of $\omega_0$ .  |
| (4) $\text{Re } Y(n\omega_0) > 0$                                       | To allow for the fact that some harmonic power is both generated and dissipated.   |
| (5) $H(n\omega_0) = \begin{cases} 1, & n = 1 \\ 0, & n > 1 \end{cases}$ | A single frequency output is desired, where $H(n\omega_0)$ is the power transfer function of the network between the terminal reference planes $T_1$ and $T_3$ . |

(b) Carroll's theory, supported by experimental measurements on triggering waveforms shows that for good TRAPATT operation  $\text{Im } Y(n\omega_0)$  must be positive and increase monotonically. A plot of  $\text{Im } Y(n\omega_0)$ , calculated as described above, vs harmonic frequency is shown in Fig. V-5.



- (c) Good TRAPATT performance<sup>33</sup> is obtained experimentally and in computer simulations when a small circuit susceptance is presented in the vicinity of the 2nd harmonic,  $2f_0$ . This small susceptance demands that a high 2nd-harmonic voltage be developed if current flows at  $2f_0$ . Such a current will be present, since the active diode is a nonlinear element and will develop a 2nd-harmonic current from the input (signal) frequency. High voltages at the 2nd harmonic aid the development of the large voltage swings which are required to trigger the ASF, especially if the TDT mechanism is not present.
- (d) The slope reactances ( $dX/d\omega$ ) at all frequencies should be minimized, i.e., the tuning elements should be located as close as possible to the diode terminals.

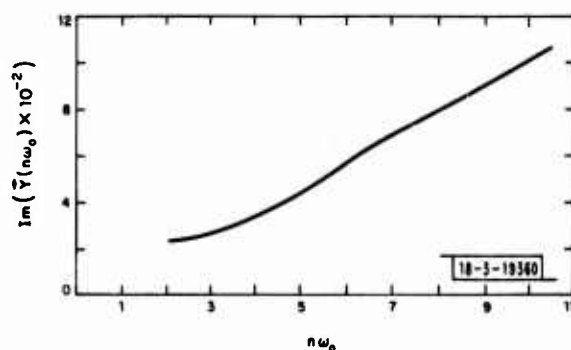


Fig. V-5. Harmonic reactance behavior of wideband TRAPATT amplifier.

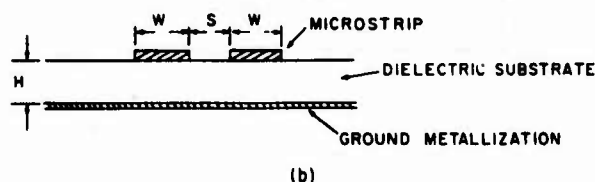
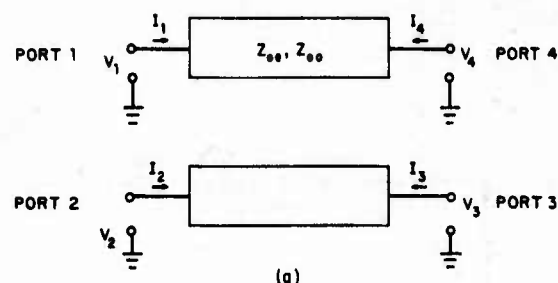
Two types of TRAPATT amplifier circuits have been developed at various industrial laboratories that exhibit wideband TRAPATT amplification. The first wideband circuit, originally developed at RCA and used by both Sperry and Hughes, utilizes a distributed coupled-line microwave circuit as the filter network. A recent wideband circuit developed by Sperry uses a circuit comprised essentially of lumped circuit elements. Both typical amplifier circuits are capable of 5 percent or better bandwidth performance with a variety of different types of TRAPATT devices.

To be useful, amplifiers must simultaneously exhibit high power, high efficiency, and broad bandwidth. Like many other microwave solid-state devices, TRAPATT diodes develop high power at low impedance levels, where the circuit impedance matching is difficult. Furthermore, the TRAPATT device is a multiple-frequency device and must be properly terminated at its harmonic frequencies for stable, efficient operation. Finally, the requirement for broadband amplification makes the TRAPATT amplifier circuit design task even more difficult, since proper termination must be provided not only at a set of frequencies, but over a set of frequency bands.

## 2. Coupled-Line Amplifier Circuit

A coupled-line microwave circuit is useful for wideband TRAPATT amplifiers, for such a line can provide an extremely wideband impedance transformation, even harmonic filtering,

Fig. V-6. Coupled-microstrip transformer: (a) four-port coupled-line circuit and (b) side view of coupled-microstrip circuit.



and an additional advantage of DC isolation due to the air gap between the lines. The basic structure of a coupled-line transformer is shown in Fig. V-6.

The theory of the coupled-line circuit has been shown by Collard,<sup>36</sup> and the equations are repeated here for completeness.

$$\begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} & Z_{13} & Z_{14} \\ Z_{21} & Z_{22} & Z_{23} & Z_{24} \\ Z_{31} & Z_{32} & Z_{33} & Z_{34} \\ Z_{41} & Z_{42} & Z_{43} & Z_{44} \end{bmatrix} \times \begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ I_4 \end{bmatrix} \quad (\text{V-10})$$

where

$$Z_{11} = Z_{22} = Z_{33} = Z_{44} = \frac{Z_{oe} + Z_{oo}}{2} \frac{1}{S}$$

$$Z_{12} = Z_{21} = Z_{34} = Z_{43} = \frac{Z_{oe} - Z_{oo}}{2} \frac{1}{S}$$

$$Z_{13} = Z_{31} = Z_{24} = Z_{42} = \frac{Z_{oe} - Z_{oo}}{2} \frac{\sqrt{1 - S^2}}{S}$$

$$Z_{14} = Z_{41} = Z_{23} = Z_{32} = \frac{Z_{oe} + Z_{oo}}{2} \frac{\sqrt{1 - S^2}}{S}$$

$Z_{oe}$  = even-mode impedance of the coupled line

$Z_{oo}$  = odd-mode impedance of the coupled line

$$S = j \tan \theta$$

$\theta$  = electrical length of the line.



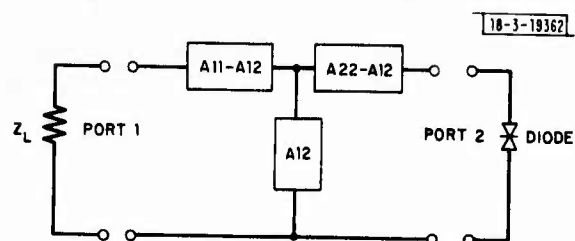
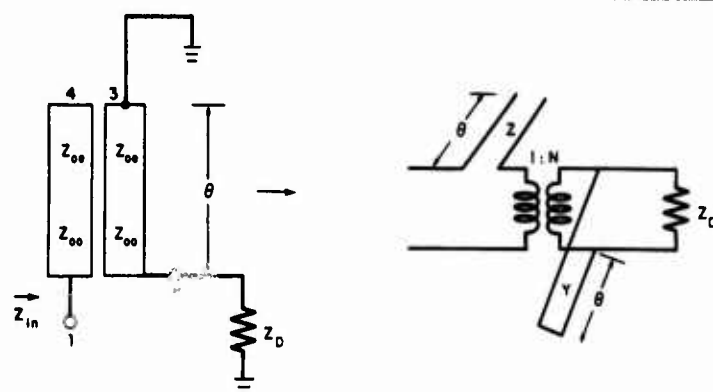


Fig. V-7. Two-port equivalent of coupled-microstrip circuit.



$$\text{WHERE } Z = \frac{2}{Y_{00} + Y_{00}}$$

$$Y = \frac{2}{Z_{00} + Z_{00}}$$

$$N = 1 + \frac{2Z_{00}}{Z_{00} - Z_{00}}$$

Fig. V-8. Coupled-line circuit and transformation.

When ports 3 and 4 are terminated with impedances  $Z_3$  and  $Z_4$ , it is possible to represent the circuit of Fig. V-6 in terms of a two-port network as shown in Fig. V-7. The elements of the equivalent circuit are defined as follows:

$$\begin{aligned}
 A_{11} &= Z_{11} - (Z_4 \times Z_{13}^2 + Z_3 \times Z_{14}^2 + Z_{14} \sqrt{1 - S^2} \Delta') / \Delta \\
 A_{12} &= Z_{12} - (Z_4 \times Z_{13} \times Z_{32} + Z_3 \times Z_{14} \times Z_{42} + Z_{13} \sqrt{1 - S^2} \Delta') / \Delta \\
 A_{21} &= Z_{21} - (Z_4 \times Z_{31} \times Z_{23} + Z_3 \times Z_{41} \times Z_{24} + Z_{24} \sqrt{1 - S^2} \Delta') / \Delta \\
 A_{22} &= Z_{22} - (Z_4 \times Z_{23} \times Z_{32} + Z_3 \times Z_{24} \times Z_{42} + Z_{23} \sqrt{1 - S^2} \Delta') / \Delta \\
 \Delta' &= Z_{33} \times Z_{44} - Z_{34} \times Z_{43} \\
 \Delta &= (Z_{33} + Z_3) (Z_{44} + Z_4) - Z_{34} \times Z_{43} \quad . \quad (V-11)
 \end{aligned}$$

In terms of these parameters, the impedance of the network at the device terminals can be calculated as:

$$Z_{in} = A_{22} - \frac{A_{12}^2}{A_{11} + Z_L} \quad . \quad (V-12)$$

A useful coupled-line circuit configuration having an open-circuited termination at port 4, a short circuit at port 3, and the input and output at ports 1 and 2, respectively, and its equivalent circuit is shown in Fig. V-8.

The equivalent circuit of the coupled-line network can be represented as the series connection of a shunt stub, ideal transformer, and series stub. If the length of the stub is chosen to be  $\lambda/4$  at the output frequency, then the coupled-line network behaves as a wideband transformer at the output frequency  $f_o$ . The transformer may be either "step up" or "step down," depending on which ports are chosen as input or output. The coupled-line network exhibits stopbands at the even harmonics and passbands at the odd harmonics. For the TRAPATT amplifier application, the TRAPATT device is connected to port 2 and the transformer is operated in the "step down" mode.

There are multiple choices of even and odd mode impedances for any specified impedance transformation ratio. A typical 10 to 1 impedance transformation with two sets of even and odd mode impedances is calculated and plotted in Fig. V-9. It is obvious that the wide-line coupled-line circuit provides a flatter frequency response for the reactive loading than the narrow-line circuit of the same transformation ratio. Broadband TRAPATT amplifiers require relatively flat frequency response at the output frequency.

Computer calculations of the depletion-layer voltage for an F-band coupled-line amplifier shown in Fig. V-10 were made at Sperry Research Center, and the waveform is shown in Fig. V-11. The calculations show that the depletion-layer voltage response to periodic impulses of current is self-consistent with the TRAPATT theory. That is, there is only one avalanche event per cycle and the product of  $C_o$  and  $dV/dt$  preceding the voltage maximum exceeds the critical current density.

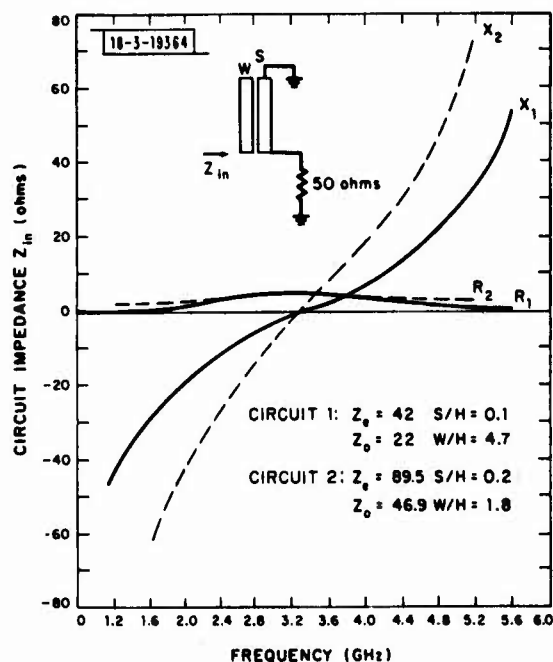


Fig. V-9. Impedance behavior of coupled-line transformers.

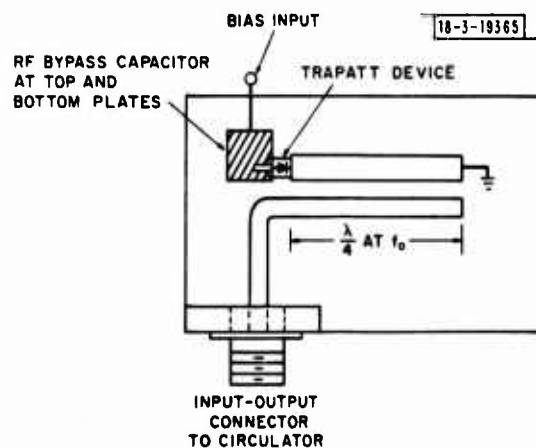


Fig. V-10. Coupled-line amplifier.

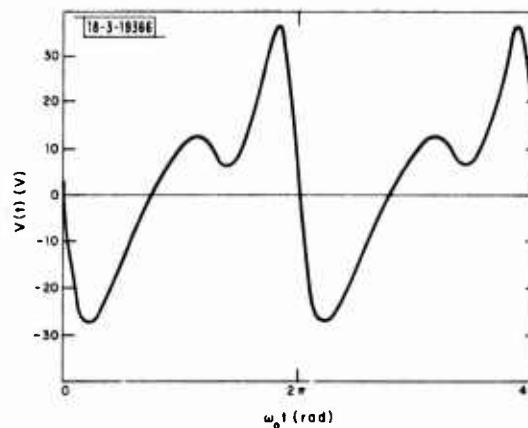


Fig. V-11. Calculated terminal voltage for coupled-line TRAPATT amplifier from Carroll model.

### 3. Lumped-Element Circuits

Broader bandwidths and higher peak power should be attainable if a less frequency-sensitive impedance-matching network were used in place of the coupled-line filter and, in fact, a lumped-element network is capable of satisfying these requirements at F-band with reduced frequency sensitivity. A lumped-element impedance-matching network was developed from the amplifier design principles described in Sec. C. The generic form of this circuit was synthesized using a computer simulation program at Sperry Research Center which calculated the gain and terminal I-V characteristic.

A simulation of the diode I-V terminal characteristic is shown in Figs. V-12 and -13. The periodic impulsive current was assumed to have a wave shape  $H(t)$ , as shown in Fig. V-12, which was modeled after current wave shapes observed from a UHF TRAPATT amplifier using sampling techniques. This driving current formed the input to the computer simulation, and the resulting voltage waveform was found to be self-consistent with the TRAPATT theory.

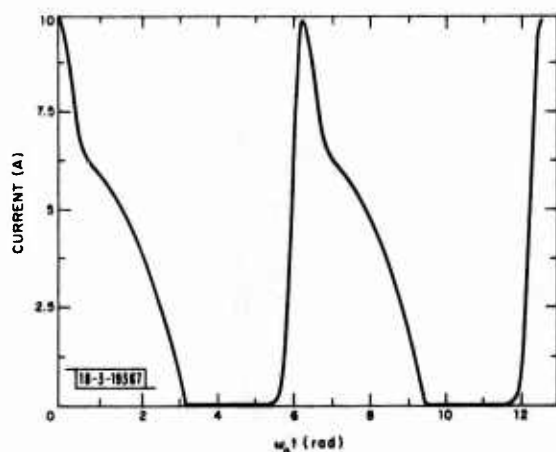


Fig. V-12. Assumed impulse current waveform.

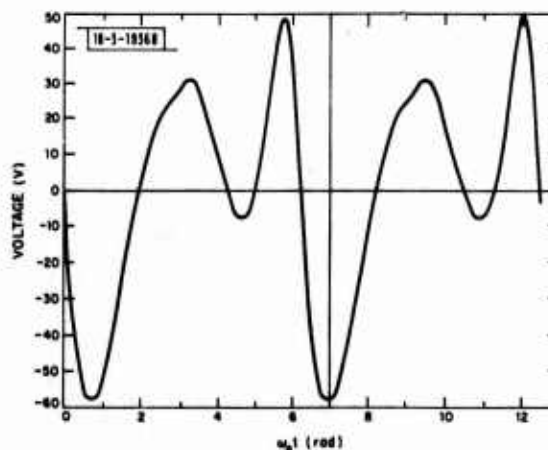
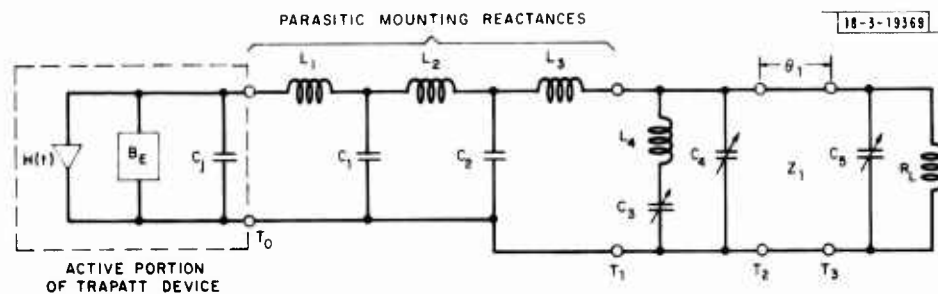


Fig. V-13. Simulation of terminal voltage waveform for 50-W wide-band lumped-element amplifier.

The final circuit components were optimized with the aid of the design principles described above. Under the constraints that the device is resistively terminated at the fundamental frequency to achieve the desired gain and reactively terminated at the harmonics, the circuit parameters were systematically varied in computer experiments. That combination of circuit components which yielded the maximum overvoltage with only one avalanche even per cycle was chosen for circuit fabrication.

The amplifier circuit was optimized for maximum gain bandwidth for large area devices which were capable of peak power performance at either 50- or 125-W levels per device. The large area diodes present most difficulty in obtaining broadband amplification, since their large-signal negative resistance is quite low ( $-R \propto 1/\text{area}$ ), and requires a greater impedance transformation, while their large junction capacitance presents higher reactance slopes. A schematic diagram of the resulting optimized lumped-element amplifier is shown in



PARAMETERS FOR 125-W AMPLIFIER

$C_1 = 4.0 \text{ pF}$	$C_3 = 2.2 \text{ pF}$	$V_B = 80 \text{ V}$
$L_1 = 0.58 \text{ nH}$	$L_4 = 0.30 \text{ nH}$	$I_{DC} = 6 \text{ A}$
$C_j = 0.249 \text{ pF}$	$C_4 = 0.30 \text{ pF}$	
$L_2 = 0.084 \text{ nH}$	$Z_1 = 50 \text{ ohms}$	
$C_2 = 0.045 \text{ pF}$	$\theta_1 = 0.86 \text{ in.}$	
$L_3 = 0.254 \text{ nH}$	$C_5 = 1.4 \text{ pF}$	

Fig. V-14. Schematic diagram of lumped-element 125-W TRAPATT amplifier.

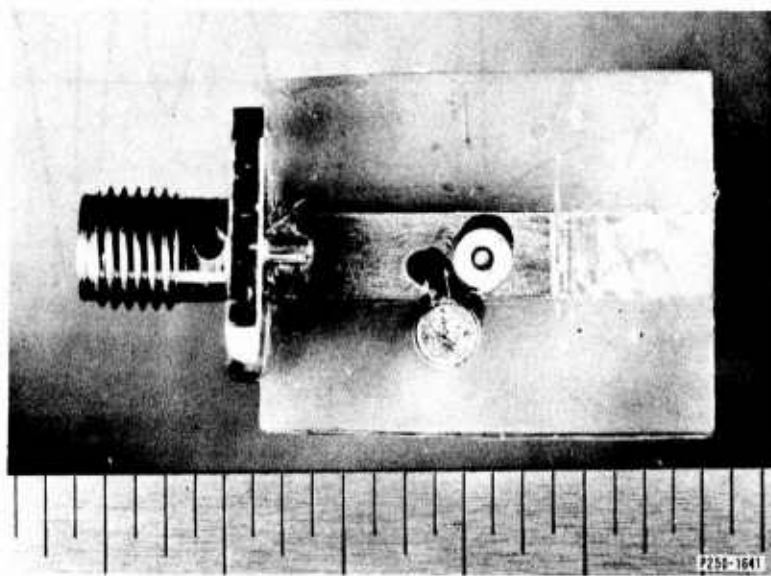


Fig. V-15. Photograph of 50-W amplifier.

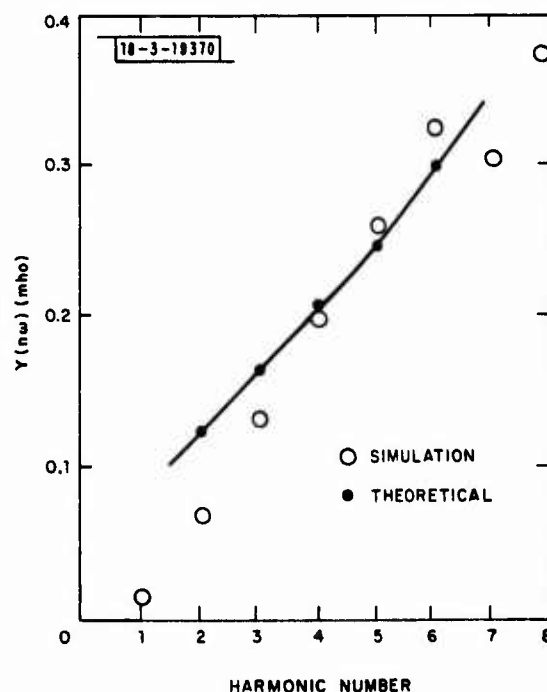
Fig. V-14, with appropriate parameters for the 125-W case. The active portion of the TRAPATT diode is represented by a periodic impulse generator  $H(t)$ , an electronic susceptance  $B_E$ , and the depletion-layer capacitance  $C_j$ . The parasitic reactances associated with the semiconductor chip mounting and connection to the external circuit are represented by the inductances  $L_1$ ,  $L_2$ , and  $L_3$  and capacitances  $C_1$  and  $C_2$ . Capacitors  $C_4$  and  $C_5$  and the shunt resonator ( $L_4 - C_3$ ) form the impedance-matching network for the amplifier. Capacitors  $C_3$ ,  $C_4$ , and  $C_5$  are variable capacitors used to tune the amplifier for optimum performance. The values of the parasitic mounting reactance were dictated by the type of diode mounting and the microwave transmission line used for the amplifier.

The 50-W amplifier was designed for microstrip using 1/16-in.-thick Tellite substrates. The devices were mounted in a varactor package and threaded into substrates, as shown in the photograph of Fig. V-15. Table V-1 shows values computed for the 50-W amplifier parameters. Note that for this case, capacitor  $C_5$  was not required. Single-tuning capacitor  $C_3$  (Johansen Model 7283) is mounted adjacent to the diode and connected via a high inductance to the 50-ohm lines. The capacitor  $C_3$  is tuned from the back of the circuit by a screwdriver adjustment. The 50-ohm line extended over the diode to provide some capacitive (this is represented by variable capacitor  $C_4$ ) tuning for the amplifier.

TABLE V-1 50-W TRAPATT AMPLIFIER PARAMETERS		
$C_1 = 2.5 \text{ pF}$	$L_3 = 0.298 \text{ nH}$	$Z_1 = 50 \text{ ohms}$
$L_1 = 0.38 \text{ nH}$	$C_3 = 2.31 \text{ pF}$	$\theta_1 = 0$
$C_1 = 0.249 \text{ pF}$	$L_4 = 0.30 \text{ nH}$	$V_B = 87 \text{ V}$
$L_2 = 0.138 \text{ nH}$	$C_4 = 0.3 \text{ pF}$	$I_{DC} = 3 \text{ A}$
$C_2 = 0.045 \text{ pF}$	$C_5 = 0$	

The computer simulation for the TRAPATT terminal I-V characteristic made use of the calculated harmonic admittance measured at terminal reference plane  $T_0$ . A plot of the admittance for the first seven harmonics is shown in Fig. V-16; also shown is a plot of the

Fig. V-16. Driving point impedance for first nine harmonics for lumped-element amplifier.





theoretical harmonic admittance calculated using Eq. (V-8). The value of  $Y_0 = 0.0355$  and the value of  $p$ , defined following Eq. (V-3), was assumed to be 0.75, which is consistent with the theoretical calculations of Carroll.<sup>35</sup> Good agreement between experimental and theoretical calculations helps to increase the confidence in the use of the Carroll model for the design of TRAPATT circuits.

#### E. HARMONIC EFFECTS

Most TRAPATT amplifiers and oscillators operate using the fundamental extraction mode; i.e., the output frequency is at the same frequency as the ASF frequency. However, it is possible to obtain energy at harmonics of the ASF frequency due to the large-signal-harmonic negative resistance of the TRAPATT.<sup>37</sup> The harmonic content of the voltage and current waveform is sufficient to extract relatively high harmonic powers. However, the efficiency of power generation will be lower for harmonic extraction than for fundamental extraction.

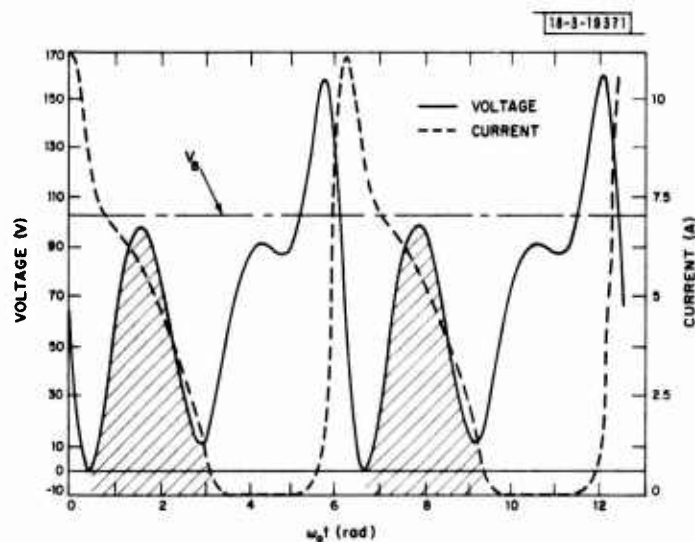


Fig. V-17. Computer simulation of the terminal voltage and current for a 2nd-harmonic extraction amplifier.

The reduced efficiency for harmonic extraction may be seen conceptually from voltage and current components necessary for maintaining waveforms which are self-consistent with TRAPATT theory. This is illustrated in Fig. V-17, which shows the computer-simulated terminal voltage and current for a 2nd-harmonic extraction F-band amplifier. The ASF frequency is 1.6 GHz and the 2nd-harmonic output frequency is 3.2 GHz. The amplitude of the 2nd-harmonic voltage is 27.9 V and the fundamental voltage amplitude is 28.6 V. The shaded area of Fig. V-17 represents power dissipation because the RF voltage is positive and the terminal current is high. The efficiency for harmonic extraction can be shown to be lower analytically than for fundamental extraction in the following manner.

The peak-to-peak amplitude of the voltage of the extracted signal is limited to the breakdown voltage to prevent multiple impact-ionization processes per cycle. The power generated by the TRAPATT is therefore limited to

$$P(n\omega_0) < \frac{V_B I(n\omega_0)}{4} [\cos \varphi(n\omega_0) + \pi]$$

where  $I(n\omega_0)$  is the harmonic amplitude and  $\varphi(n\omega_0)$  is the harmonic phase.  $P(n\omega_0)$  is negative for  $-\pi/2 < \varphi < \pi/2$  indicating power generation. The Fourier coefficient  $I(n\omega_0)$  of the 2nd harmonic of the impulse current will always be less than that of the fundamental\*  $I(n\omega_0) < I(\omega_0)$ . Therefore, for a given breakdown voltage, the 2nd-harmonic power generated will always be less than the maximum available at the fundamental. In the computer simulation shown in Fig.V-17, the fundamental extraction efficiency was 27 percent, whereas the 2nd-harmonic extraction efficiency was 12 percent.

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\*For an impulsive type waveform with nonzero width, the Fourier coefficient amplitudes decrease as  $n^{-a}$ , where  $0 \leq a \leq 2$ .

## CHAPTER VI EXPERIMENTAL RESULTS

### A. INTRODUCTION

TRAPATT amplifiers have been constructed in several distributed circuit media forms, in some cases including lumped elements as well. The degree of design sophistication has varied from pure cut-and-try techniques, using either coaxial slugs or plated ceramic chips as movable tuning elements, to exploitation of the theoretical concepts discussed in Chap. V. Some of the more significant results which have been reported are discussed in this chapter, and results of measurements made at Lincoln Laboratory also are described.

These provide representative properties which are characteristic of the best amplifiers achieved to date, and may be taken as benchmarks of the current state of the art.

### B. COUPLED-LINE AMPLIFIERS

Coupled-line pulsed TRAPATT amplifiers have been investigated at RCA, Sperry, and Hughes. These circuits have been developed using both microstrip and slab-line geometry.

The best results at RCA were obtained from a coupled-line microstrip circuit including an external idler resonator circuit as illustrated by the photograph shown in Fig. VI-1. This network, when provided with a tunable external idler, yielded some capability for broadband 2nd-harmonic amplification in F-band.

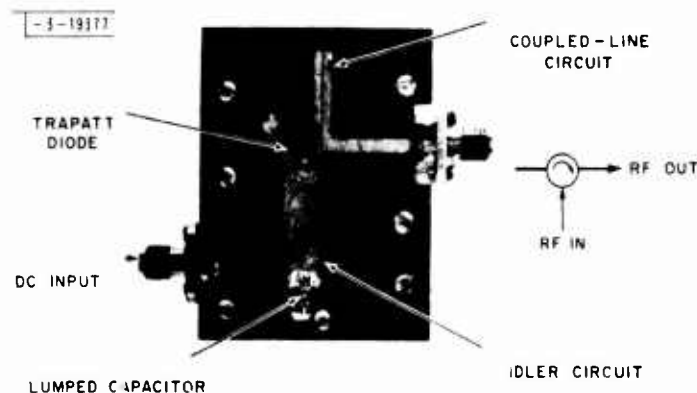


Fig. VI-1. TRAPATT amplifier with hybrid idler circuit.

The basic amplifier consists of a microstrip coupled line and hybrid idler circuit connected in series with a lumped-variable capacitor to ground. The resonant frequency of the idler circuit was tunable from 1.3 to 3.8 GHz, by means of capacitance adjustment. The coupled-line impedance-matching transformer matched the diode impedance to the 50-ohm load at the output frequency. A photograph of a broadbanded version of this circuit is shown in Fig. VI-2. In order to reduce the parasitic effects associated with a packaged device, an unpackaged TRAPATT diode was mounted in chip form. The diode was mounted at the end of a gold-plated brass stud by means of a conductive silicon heat sink compound, and the stud was then inserted into the circuit from the back of the supporting block to insure good electrical contact with the back of the microstrip line.

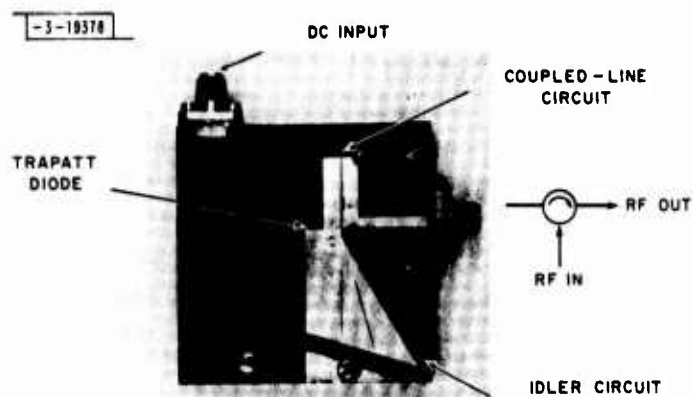


Fig. VI-2. Broadband coupled-line amplifier.

TABLE VI-1 SUMMARY OF RESULTS <sup>38</sup>			
	Single Diode KR9D No. 5	Single Diode KR9D No. 2	Two-Diode Stack KR9D
Power Output (W)	82	83	166
Bandwidth (percent)	9 (1 dB)	narrow	3.09 to 3.14 (3 dB)
Gain (dB)	4.9	6.3	7.55
Pulse Width ( $\mu$ sec)	10	50	10
Efficiency (percent)	15	10.5	10.15

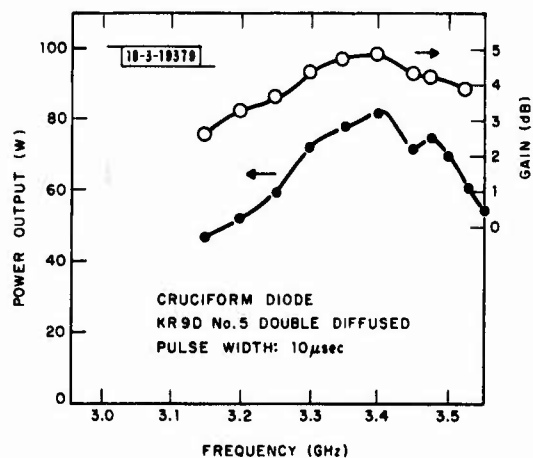


Fig. VI-3. RCA S-band TRAPATT amplifier properties.

The best results reported for the coupled-line idler circuit are summarized in Table VI-1. Wideband amplification was obtained over the 3.25- to 3.55-GHz frequency band (as illustrated by the passband shown in Fig. VI-3). A maximum pulsed output power of 82 W, with a peak mid-band gain of 4.9 dB was obtained using a pulse width of 10  $\mu$ sec.

The best power-added amplifier efficiency of 14.7 percent was obtained using a current profiled across the frequency of operation. At 3.25 GHz, the current was 4.5 A and was increased to 6.5 A at 3.55 GHz. In addition, RCA has achieved a maximum output of 166 W using a two-diode series stack with a maximum gain of 7.55 dB. Power-added efficiency was 10.15 percent with a 10- $\mu$ sec pulse width (see Fig. VI-4).

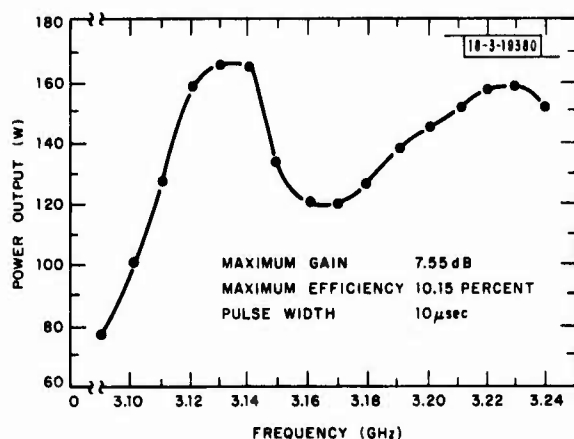


Fig. VI-4. RCA two-diode power frequency characteristics.

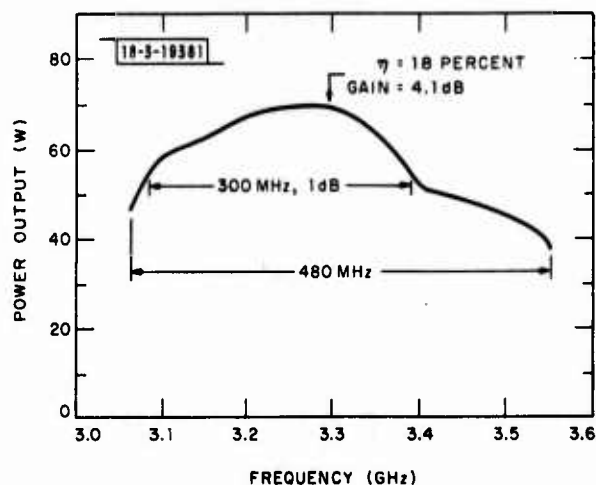


Fig. VI-5. Performance of double-diffused-mesa TRAPATT amplifiers.

RCA also has observed up to 195 W from a single diode at a power-added efficiency of 20 percent and maximum gain of 6.27 dB across a narrow bandwidth.

Double-diffused-mesa diodes were reported to provide amplification with 300-MHz 1-dB bandwidth centered at 3.3 GHz. The peak output power was 70 W at 18-percent efficiency, and midband gain was 4.1 dB, as shown in Fig. VI-5. Similar power levels, bandwidths, and efficiencies have been achieved using variations of the coupled-line circuit at both Sperry Research Center and Hughes' Torrance Research Center.

The Sperry Research Center also has investigated a slab-line geometry coupled-line amplifier circuit. In this circuit, the TRAPATT device is mounted in a varactor package located at the output port of the coupled-line network, as shown in Fig. VI-6. The parasitic lead inductance of the TRAPATT package was chosen to optimize the amplifier performance.

Under low-power pulsed operation, a -1-dB bandwidth of 300 MHz was obtained with a nominal gain of 6 dB, as illustrated in Fig. VI-7 (Ref. 24). The power-added efficiency of the amplifier was reported to be 20 percent at midband. Computer calculations showed good agreement with the measured passband. The broad bandwidth was attributed to the diode being resonated at the output frequency by the parasitic diode mounting reactance. This eliminates the long-lines effect of tuning on the output of the coupled-line network.

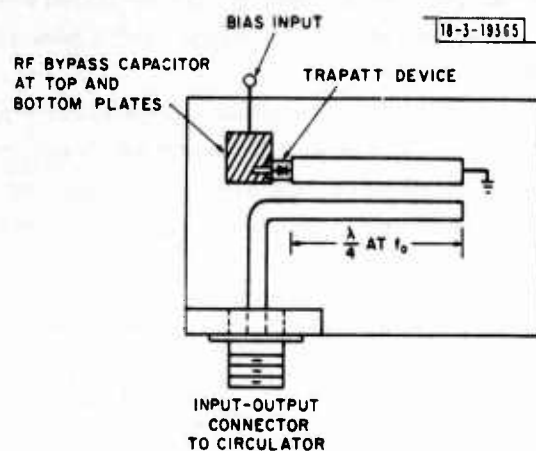


Fig. VI-6. Coupled-line amplifier.

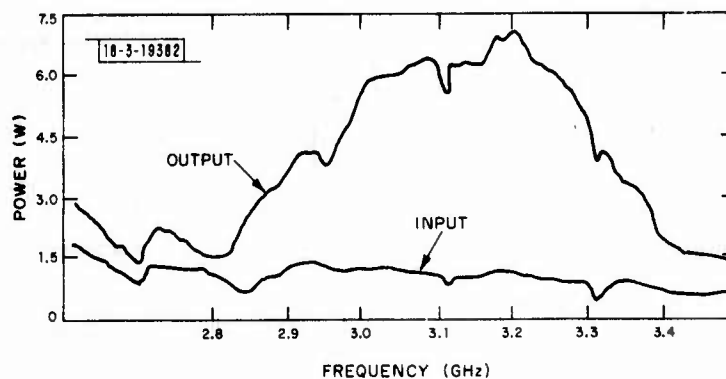


Fig. VI-7. Measured passband for coupled-line TRAPATT amplifiers.

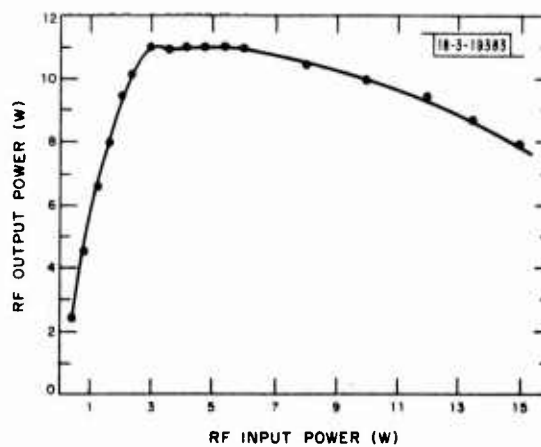


Fig. VI-8. Typical input-output power characteristics of TRAPATT amplifiers.



TRAPATT amplifiers are large-signal amplifiers and do not exhibit net gain until the input signal amplitude exceeds a critical threshold value. For signal levels below the critical threshold value, the TRAPATT diode presents a relatively good impedance match to the circulator, and the amplifier exhibits a loss. When the input signal level exceeds a critical threshold, net gain is observed. There is a small dynamic range where the amplifier is linear (3 to 5 dB). At higher input power levels, the amplifier saturates, and the output power remains constant and then decreases. This is illustrated in Fig. VI-8 which shows the input-output power characteristics measured for a typical low-power S-band coupled-line amplifier.

#### C. EXPERIMENTAL LARGE AREA DIODE AMPLIFIERS USING LUMPED-ELEMENT CIRCUITS

Wideband amplification has been obtained at both the 50- and 100-W power levels using a lumped-element microstrip circuit developed at the Sperry Research Center from the amplifier design principles described in Chap. V. A photograph of the lumped-element amplifier is shown in Fig. VI-9.

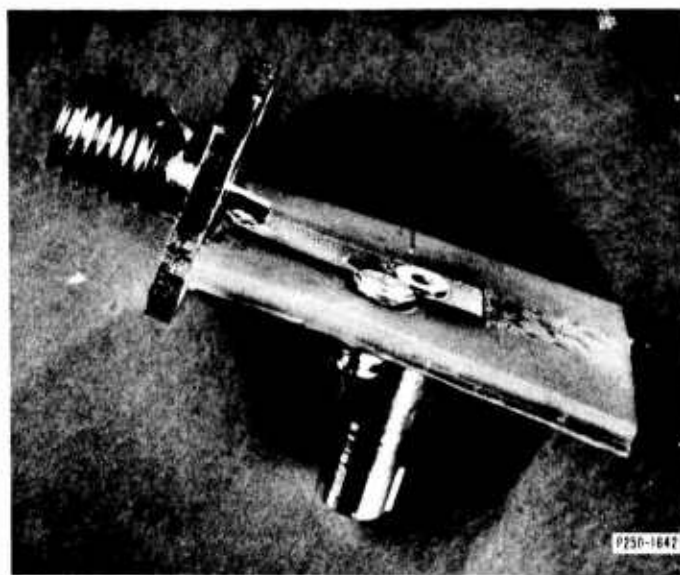


Fig. VI-9. Lumped-element 50-W TRAPATT amplifier.

The 50-W amplifier was a microstrip circuit design on Tellite substrate including lumped elements as described in Sec. D. Diode capacitance at breakdown was approximately 2.5 pF, and a -1-dB bandwidth of about 300 MHz was obtained for a nominal midband gain of 6 dB. Sperry's reported results are illustrated in Fig. VI-10. The peak output power was 50 to 60 W for a 1- $\mu$ sec pulse width at a 0.001-percent duty factor.

The measured passband agreed well with the calculated passband, assuming that the diodes may be represented as a frequency-independent negative resistor over the frequency range of interest. The broad bandwidth is attributed to the fact that all tuning is accomplished with lumped elements in the vicinity of the device, thus reducing the long-line effect of distributed circuits.

Long pulse operation with the lumped-element amplifier has been obtained using 2.5-pF capacitance diodes of a ring geometry mounted on diamond heat spreaders. Peak pulsed powers

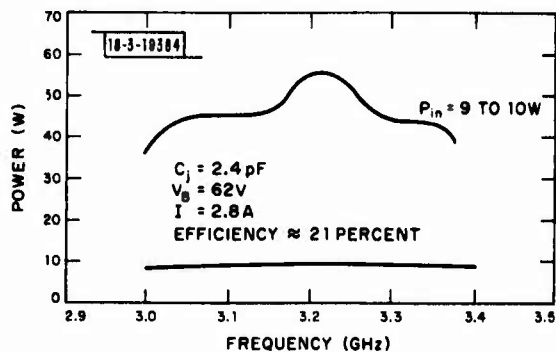


Fig. VI-10. Passband of Sperry 50-W amplifier.

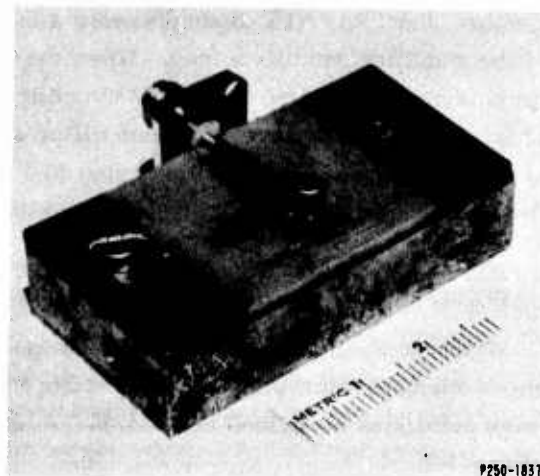


Fig. VI-11. Lumped-element 125-W amplifier.

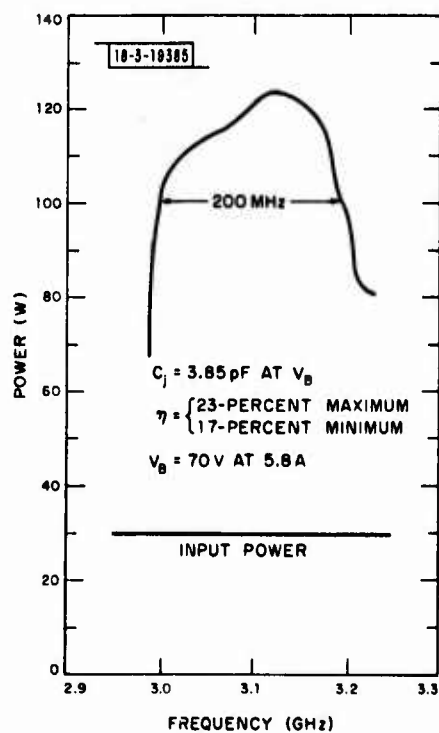


Fig. VI-12. Passband of Sperry 125-W amplifier.

at the 30- to 40-W level have been measured using 50- $\mu$ sec pulses at a 0.001 duty factor. Higher duty factors were not attempted; no forced cooling was used. The midband gain was 5 dB, and the efficiency was  $\sim$ 20 percent.

Peak output powers of  $\sim$ 125 W have been obtained using larger area diodes (4.0-pF capacitance at breakdown). The lumped-element circuit was modified to include a third tuning capacitor  $C_5$ . A photograph of this amplifier is shown in Fig. VI-11. This tuning capacitor is located approximately a quarter wavelength away from the TRAPATT device and serves as an impedance-matching function to help present the required circuit impedance to the reduced negative resistance of the larger area devices.

The larger area devices were reported to be capable of saturated peak output powers of 100 to 125 W at a midband gain of 5 dB and a  $-1$ -dB bandwidth of 200 MHz. The midband power-added efficiency was approximately 23 percent. The passband of a typical amplifier using inverted complementary devices ( $n^+$ -p- $p^+$ ) is shown in Fig. VI-12. The reduced bandwidth is attributed to the difficulty in matching the load to the reduced value of the large-signal negative resistance associated with the larger area devices.

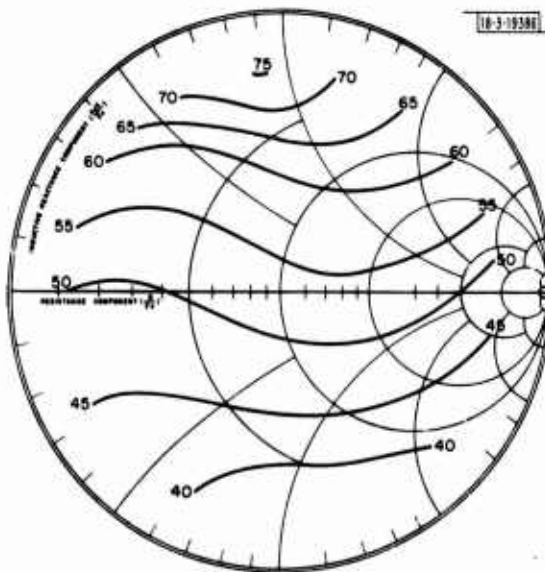
Amplifier results were obtained using inverted complementary ( $n^+$ -p- $p^+$ ) type devices rather than the conventional  $p^+$ -n- $n^+$  devices. The  $-1$ -dB bandwidth was generally 20 percent greater with the  $n^+$ -p- $p^+$  devices.

#### D. DEPENDENCE ON OUTPUT LOAD

The output characteristics (fundamental and 2nd-harmonic power phase variations) of the 50-W lumped-element TRAPATT amplifier have been measured as a function of load impedance at RADC by D. W. Griffin.<sup>39</sup> The technique involved presentation of a return loss controllable in magnitude and phase, and measurements of incident and transmitted power levels, outside the amplifier circulator.

The RF output power was found to depend upon the load impedance presented to the circulator at the fundamental operating frequency, as illustrated in Fig. VI-13. Equipower contours are shown in watts for the 50-W nominal amplifier operating with 15-W RF input power. The

Fig. VI-13. Power of fundamental wave output of S-band TRAPATT amplifier as a function of load impedance. Equipower contours in watts; signal frequency = 3.2 GHz; incident power = 15 W peak; signal pulse length = 1.0  $\mu$ sec; prf = 1 kHz; and duty factor = 0.1 percent.



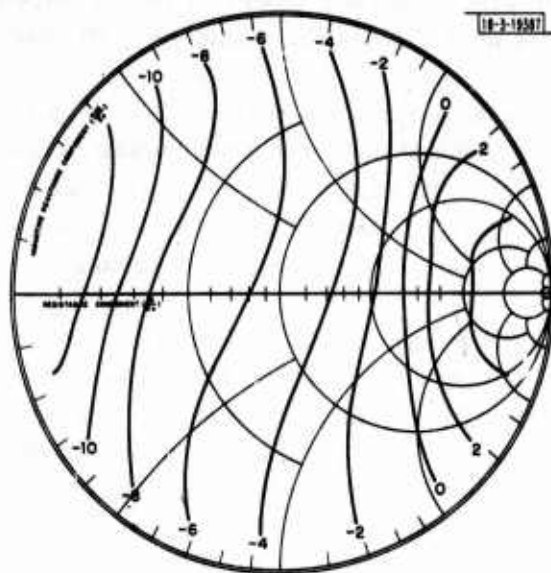


Fig. VI-14. Relative phase of fundamental wave output of S-band TRAPATT amplifier as a function of load impedance. Equiphas contours in electrical degrees; signal frequency = 3.2 GHz; incident power = 15 W peak; signal pulse length = 1.0  $\mu$ sec; prf = 1 kHz; and duty factor = 0.1 percent.

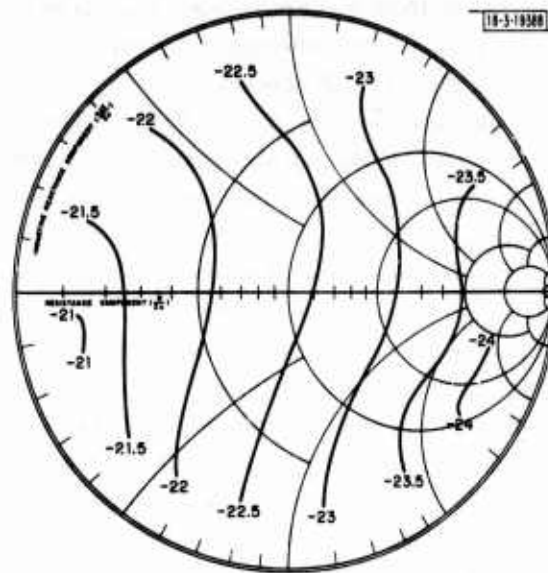


Fig. VI-15. Power of 2nd-harmonic wave output of S-band TRAPATT amplifier as a function of load impedance. Equipower contours in decibels below fundamental; signal frequency = 3.2 GHz; incident power = 15 W peak; signal pulse length = 1.0  $\mu$ sec; prf = 1 kHz; and duty factor = 0.1 percent.

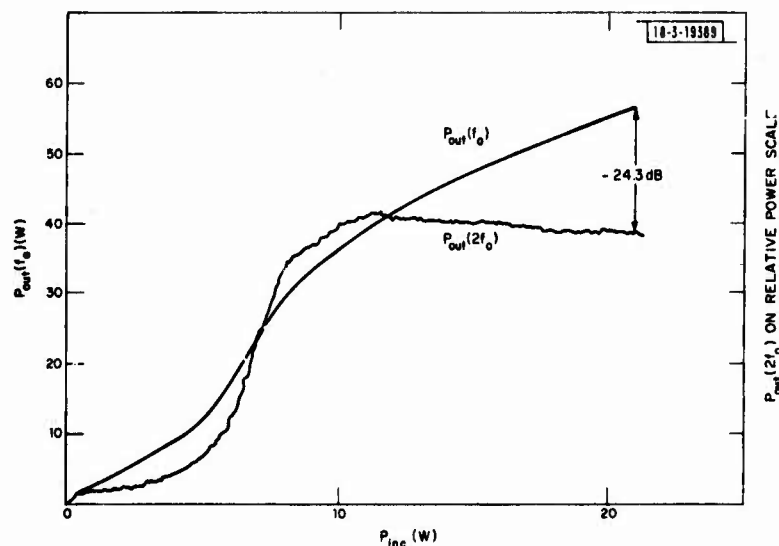


Fig. VI-16. Fundamental and 2nd harmonic vs incident power for 50-W S-band TRAPATT amplifier.  $V_B = 60$  V;  $I_B = 3$  A; attenuation = 20 dB; VSWR = 1.02;  $f_o = 3.2$  GHz; pulse length = 1  $\mu$ sec; prf = 1 kHz; and duty factor = 0.1 percent. Assembly using two 3-port circulators.

fundamental output power varied from 40 to 75 W depending upon the impedance. For a 1.5:1 load VSWR, the RF power varied from 50 to 55 W. The phase characteristics of the 50-W amplifier are shown in Fig. VI-14, which shows the equiphase contours in electrical degrees for an amplifier operating at 3.2 GHz. The maximum amplifier phase variation for a 1.5:1 VSWR was 2°.

The 2nd-harmonic output was also measured as a function of the input power level and load impedance. Figure VI-15 shows the equipower contours of the 2nd-harmonic output in decibels below the fundamental. The 2nd-harmonic output was less than -21 dB below the fundamental in the worst case and varied from -21 dB for a low-impedance load to -24 dB for a high-impedance load. Figure VI-16 shows the 2nd-harmonic output as a function of fundamental input power. Under matched conditions, the 2nd-harmonic output was -24.3 dB below the fundamental output. The 2nd-harmonic output power did not increase with input power but leveled off and remained constant for input power levels greater than 10 W as illustrated in Fig. VI-16. This characteristic also was measured for the two-capacitor 100-W TRAPATT amplifiers. Figure VI-17 shows the power output at  $f_0$  and  $2f_0$  as a function of input level, and reveals that the 2nd-harmonic output is independent of input and is -51 dB below the rated output.

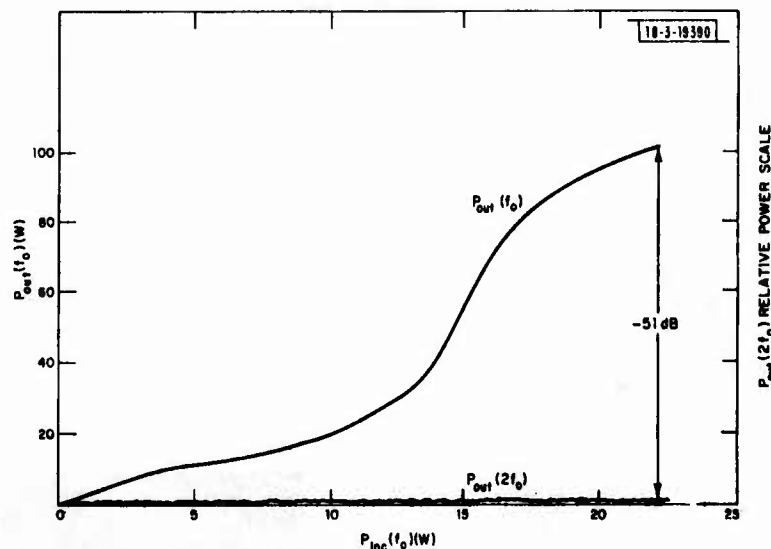


Fig. VI-17. Fundamental and 2nd harmonic vs incident power for 125-W S-band TRAPATT amplifier.  $V_B = 70$  V;  $I_B = 6$  A; attenuation = 20 dB; VSWR = 1.02;  $f_0 = 3.2$  GHz; pulse length = 1  $\mu$ sec; prf = 1 kHz; and duty factor = 0.1 percent. Assembly using two 3-port circulators.

#### E. LINCOLN MEASUREMENTS

Lincoln Laboratory has carried out a measurement and development program for S-band TRAPATT amplifiers and oscillators for the past several years. In general, these measurements support the characteristics described above for both coupled-line and lumped-element circuits. A detailed characterization of a 50-W lumped-element amplifier procured from Sperry was undertaken, motivated by its reportedly high power-added efficiency over a wide bandwidth. Measurements included the dependence of phase shift on frequency, input power, and time after pulse turn on, as well as gain, bandwidth, and efficiency, and are described in detail in Sec. 1 below.

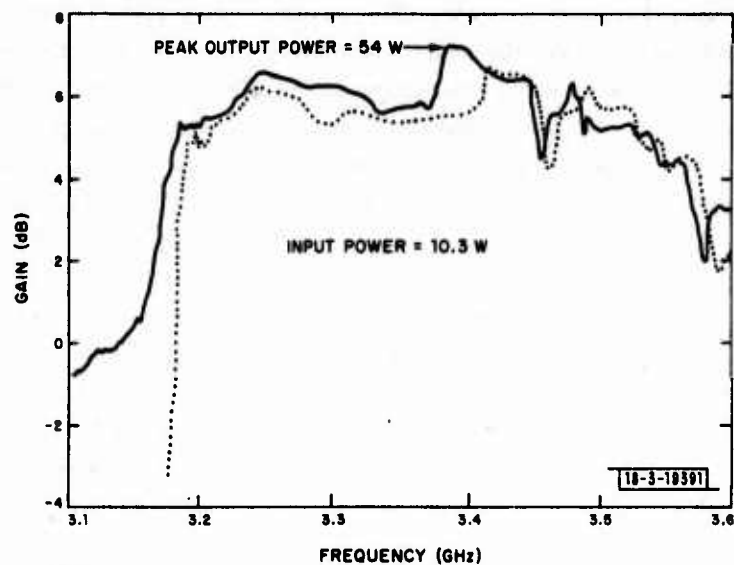


Fig. VI-18. Bandpass characteristics of the Sperry 50-W amplifier delivered to Lincoln Laboratory.

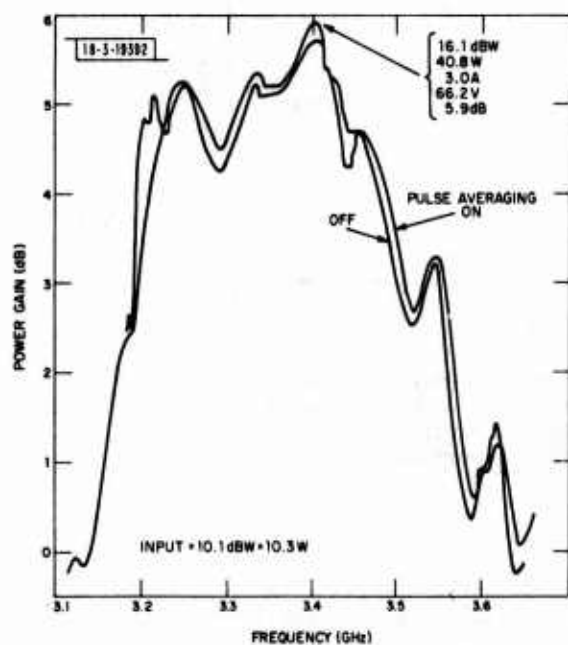


Fig. VI-19. Lincoln measurement of Sperry 50-W amplifier bandpass characteristics.

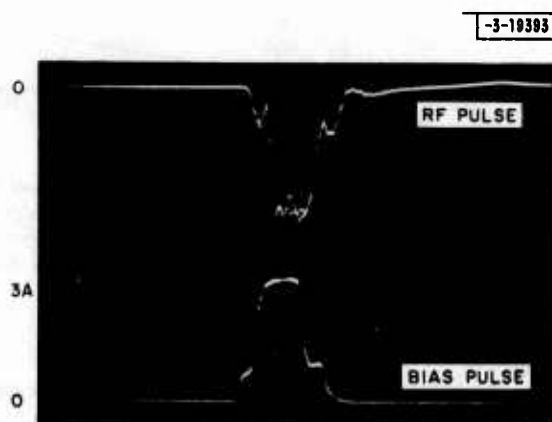


Fig. VI-20. Bias current and video-detected output pulses.



In addition, a distributed element synthesis technique based upon experimental measurements was developed with results which indicate that control of fundamental, 2nd, and 3rd harmonics alone can yield efficiencies above 25 percent, and that the circuit dominant nature of the TRAPATT phenomena does permit device interchangeability without additional tuning. This program is described in Sec. 2.

#### 1. Lincoln Measurements on the Sperry 50-W Lumped-Element Amplifier

A number of amplifier and diode combinations were tested at Lincoln Laboratory by Sperry personnel using equipment which permitted continuous measurement of gain as a function of swept frequency across most of S-band. The circuit which gave the "best" results was delivered to Lincoln Laboratory with the particular diode used in obtaining these results still mounted in the circuit. This diode was a  $p^+-n-n^+$  conventional (nonring) mesa. The circuit was essentially identical with that shown in Fig. V-14, with element values given by Table V-1.

Bandpass characteristics of this circuit-diode combination are presented in Fig. VI-18, as delivered. The tracings represent an input power level of 10.3 W measured at the frequency of highest output power and at two different adjustments of the tunable capacitor. At higher inputs, there was a suspicion that excessive saturation of the amplifier was occurring. For both traces, the DC bias input was nominally 3.0-A current and 60-V operating voltage measured at the frequency of maximum output power. The bias current and operating voltage are sensitive to input frequency and power, since these affect the TRAPATT mode waveforms in a nonlinear fashion.

Subsequently, Lincoln measurements were made with all known circuit losses and frequency dependencies calibrated out. Figure VI-19 shows the passband response of the amplifier under these conditions, with the input power set at 10 dBW. The peak midband gain was 6 dB corresponding to a peak output power of 40.8 W. The midband power-added efficiency was 15 percent.

The RF pulse width was 1.5- $\mu$ sec long at a 1-kHz repetition rate. The video bias pulse width was 1- $\mu$ sec long superimposed upon a 1.5- $\mu$ sec RF pulse, as illustrated in Fig. VI-20, which shows the video-detected output and bias current at 3.4 GHz. Note that the device draws some current,  $\sim 0.75$  A under the influence of the RF drive and the bias source impedance. RF gain results when the bias source drives the operating current to its 3.0-A peak value. Adjustment of the bias source impedance to a low enough value ( $\sim 6$  ohms for this diode) can allow the RF-induced reduction of the operating voltage to trigger the full operating current. Hence, a pulse bias supply is unnecessary and class "C" operation is possible with TRAPATT devices. This was not attempted with the Sperry amplifier, although it has been demonstrated by RCA.<sup>34</sup>

The uniformity of the output power across the pulse was measured using a 100-nsec window. The power output variation was less than 0.2 dB across the pulse at midband degrading to 0.4 dB at the band edges, as illustrated by the data given in Table VI-2. For these measurements, the input power level was 10.0 W, which yielded a clean pulse shape at each of the measurement frequencies.

The amplifier was biased from a constant voltage source through a 50-ohm series resistor. The bias current, variation, and power output were measured as a function of frequency when the amplifier was operated at a nominal input power level of  $10.5 \pm 0.5$  dBW. Point-by-point measurements of power output, bias current, and input power level are shown in Fig. VI-21. The bias current varied from 2.8 A at the high end of the band to 3.1 A near the low end of the band. The measurement indicates that current profiling is not necessary for wideband operation. Achievement of broader bandwidth by utilizing current profiling has been suggested;

TABLE VI-2				
PULSE POWER PROFILE				
[Output Power (dBW) in a 100-nsec Measurement Window]				
Time after Turn-On ( $\mu$ sec)	Frequency (GHz)			
	3.25	3.3	3.35	3.4
0.0	14.9	15.2	15.6	15.4
0.1	15.0	15.3	15.6	15.3
0.2	15.0	15.3	15.6	15.3
0.3	14.9	15.3	15.55	15.3
0.4	14.9	15.2	15.5	15.3
0.5	14.8	15.2	15.4	15.3
0.6	14.8	15.1	15.4	15.3
0.7	14.7	15.0	15.4	15.3
0.8	14.7	15.0	15.4	15.2
0.9	14.6	15.0	15.4	15.2
1.0	14.6	15.0	15.4	15.25

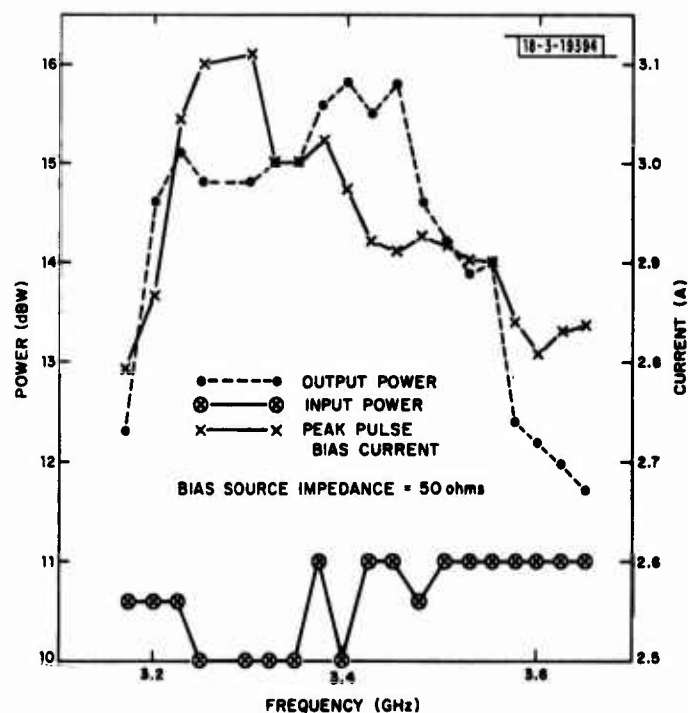


Fig. VI-21. Output power and bias current dependence on operating frequency for fixed-bias source impedance.

however, repeating the measurements under constant current conditions produced little change in the passband response. In fact, at 3.2 GHz, increasing the bias current at 2.9 A resulted in missing pulses or breakups of the RF amplification. This is illustrated in Fig. VI-22 which shows the video-detected output power and the bias current at the lower band edge. The reason for this breakup is not presently understood, but this phenomenon appears to inhibit the bandwidth at the lower frequency end. The implications of this phenomenon for broadband amplification under class "C" conditions are not known.

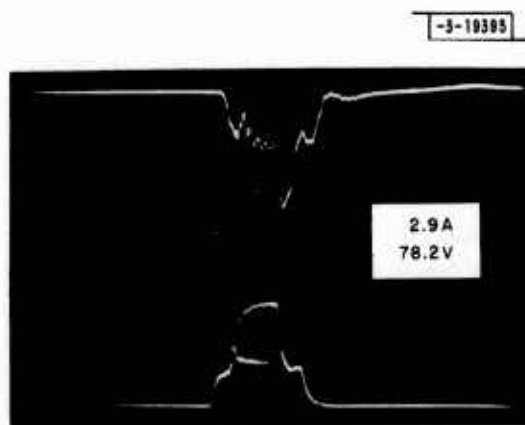


Fig. VI-22. Instability observed on detected bias and RF pulses at increased bias currents.

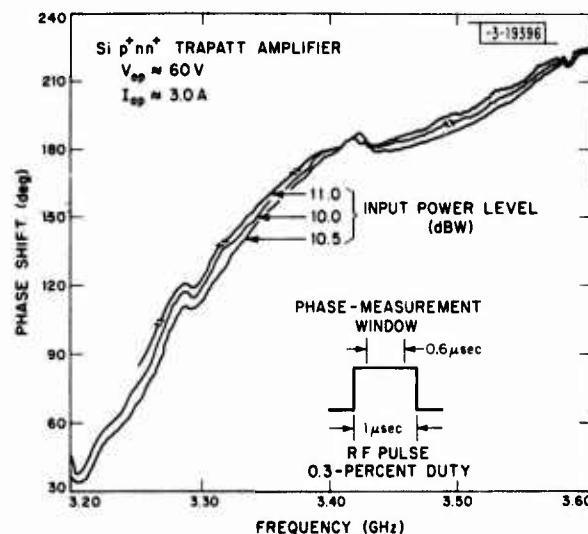


Fig. VI-23. Phase shift vs frequency for several levels of input power.

The phase response of the TRAPATT amplifier was measured as a function of both frequency and input power level. The phase shift was measured using a 600-nsec window centered in a 1-μsec RF pulse. The shape of the phase vs frequency curve, shown in Fig. VI-23, exhibited a deviation from linearity of  $\sim 6^\circ$  from the best straight-line fit. The phase shift appears to be characterized as piecewise linear with a slightly lower slope at frequencies above the gain peak at 3.4 GHz. The phase shift is not strongly dependent upon the input power, over the variation of  $\pm 0.5$  dB which was applied. Figure VI-24 shows the results of narrowing the phase-measurement window to 100 μsec, and sampling the phase shift at several values of time delay from the leading edge of the pulse. The phase shift across the RF pulse varied from a maximum of  $10^\circ$  at the low end of the band to less than  $2^\circ$  above midband. A  $\pm 15^\circ$  ripple component is found on the high-frequency side of the passband. Since the phase shift and the ripple are not strongly dependent upon the time delay from the leading edge of the pulse, its absence from Fig. VI-23 suggests a measurement system ripple at the narrower measurement window. This 100-nsec window is the lower limit for the pulsed phase-measurement system, and the ripple magnitude should probably be interpreted as corresponding to error bars on the measurement accuracy. For the wider measurement window in Fig. VI-23, an accuracy of  $\pm 5^\circ$  is expected.

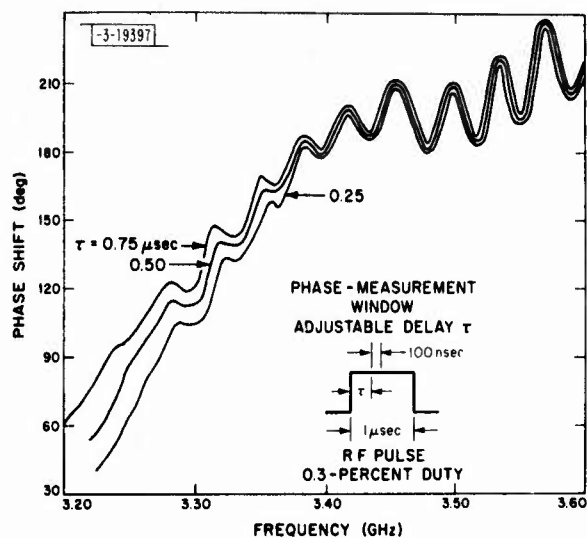


Fig. VI-24. Phase shift vs frequency for several measurement delays from pulse leading edge.

## 2. A Fixed-Tuned TRAPATT Amplifier Synthesis Procedure

In the case of TRAPATT diodes, there are complications which limit the ability to design and analyze amplifiers. Theoretical models of the device usually assume a particular, normally simple, current waveform to compute a voltage response. Sampling measurements indicate complex current waveforms which many existing analyses cannot treat. The more exact computer simulations are very expensive in terms of computer time and have not been run for more than a very few cases. Finally, the high current density and large ionization parameters which characterize the mode lead to instabilities in the numerical methods used to compute solutions. Thus, there is not a very large body of accumulated theoretical chip admittance data for these devices, in contrast to the situation with IMPATT diodes. Data on the behavior of the mode admittance with increasing RF voltage is virtually nonexistent and, in addition, the high degree of nonlinearity which characterizes the operation of this device requires that the circuit not only provide the proper impedance at the desired operating frequency, but at several harmonics as well.

While the techniques described in Chap. V have worked well, they are of recent vintage, are motivated by attempts to increase bandwidth, are rather complicated to design and construct, and do not entirely obviate the need for externally tuning the final product.

As a result, most early TRAPATT amplifiers and oscillators were designed by empirical methods, involving a great deal of experimental tuning. A useful circuit for this purpose has been described by Evans<sup>32</sup> and consists of a coaxial air line with a number of coaxial tuning sleeves as shown in Fig. VI-25. It has generally been found that one coaxial tuner adjacent to

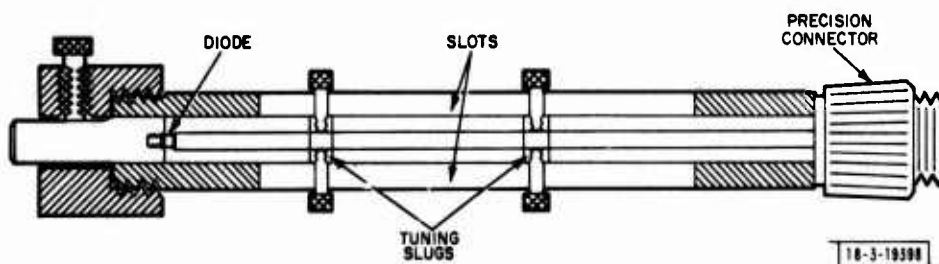


Fig. VI-25. Evans-type coaxial TRAPATT circuit.

the packaged diode and several tuners at a distance approximately  $\lambda/2$  from the diode work well as a free-running oscillator. The characterization of this circuit led Evans to formulate the TDT theory of self-starting TRAPATT oscillation, as described previously.

Once an oscillator has been constructed from a circuit such as the one described above, the diode and cavity end plane can be replaced by a 50-ohm probe, enabling the measurement of impedances seen by the packaged diode. A fixed-tuned simple RF circuit which provides the same impedances through several harmonics but a different real part at the fundamental might provide stable amplification. Early experimental work at Lincoln Laboratory investigated such approaches to TRAPATT amplifier design, and a useful synthesis technique was developed with several interesting results.

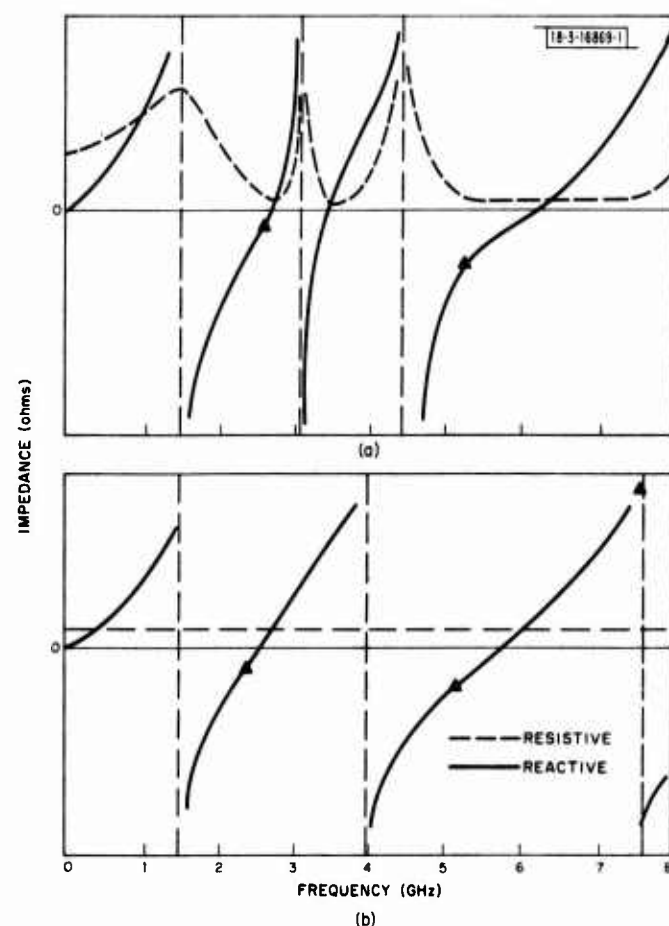


Fig. VI-26. TRAPATT load impedance characteristics: (a) measured TRAPATT load and (b) simplified load.

Figure VI-26 indicates the results of an impedance measurement on a circuit which supported efficient oscillation by a particular TRAPATT diode in a threaded pill varactor package, for measurements between DC and the 3rd harmonic. The oscillator frequency was 2.65 GHz for this case and the triangles indicate measured reactances at fundamental, 2nd, and 3rd harmonics. Fifty watts of free-running peak output power were obtained at 35-percent efficiency with 1.0- $\mu$ sec pulses at 1-percent duty. Since only harmonically related impedances can have

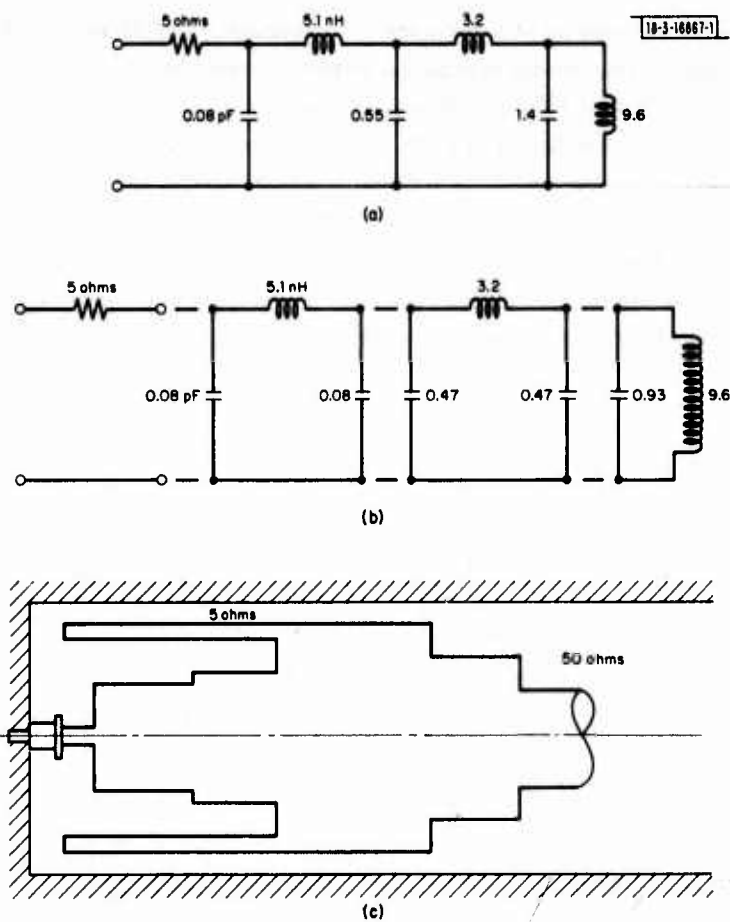


Fig. VI-27. Synthesis of distributed TRAPATT load: (a) lumped element, (b) alternate configuration, and (c) coaxial realization.

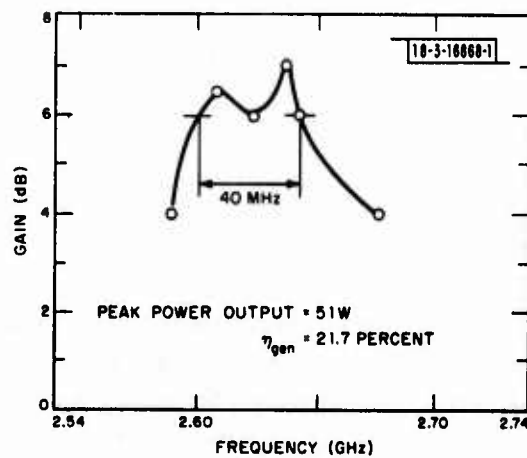


Fig. VI-28. TRAPATT locked gain-bandwidth performance.



any influence on a periodic waveform, the argument can be made that impedance behavior at frequencies between the harmonics is unimportant. This may be used to simplify the required load behavior, and in Fig. VI-26(b), the impedance behavior for the simplest physically realizable lumped-element passive network with the correct reactances at fundamental, 2nd, and 3rd harmonics are shown. The *a priori* conditions were imposed that: (a) harmonics above the 3rd would not be considered since their inclusion was believed to compound the circuit complexity too much for any useful amplifier, and (b) real parts could be approximated by a constant series resistance, i.e., sharp narrow peaks at the reactance poles were neglected, for a similar reason.

Synthesis of a lump-element L-C ladder with the required behavior is straightforward<sup>40</sup> and leads to a network as shown in Fig. VI-27(a). Five ohms of resistance have been added in series. In Fig. VI-27(b), symmetrical pi-networks are cascaded in an alternate configuration, and since each of these has a distributed element realization as a length of transmission line, a coaxial realization of such a network may be designed and would appear similar to Fig. VI-27(c). The magnitude of the real part, shown as 5 ohms in the figure, is independently controlled by the characteristic impedance of the outer coaxial section, while the reactive behavior is controlled by the inner section. This form of bifurcated coaxial lines effectively places the two in series at a reference plane slightly offset from their physical confluence.<sup>41</sup>

Such a circuit was designed, constructed, and operated as a 2.64-GHz oscillator. Many diodes of differing area, doping level, depletion width, and breakdown voltage, from several different manufacturers, were utilized. No tuning adjustments were provided. The only parameter common to all the diodes tested was their style of package, the threaded pill commonly used for microwave varactor diodes. The oscillation frequency was precisely 2.64 GHz in each case, although bias voltage, current, output power, and efficiency were different. In all cases, the oscillator efficiency was above 20 percent. The original diode, a GE silicon p-n-n<sup>+</sup> with an 80-V breakdown, produced 50 W at 35 GHz, just as in the original Evans-type tunable circuit.

Circuits designed to present a larger real part impedance also have been constructed, by modifying the ratio of outer conductor radius to that of the intermediate coaxial wall. For a 10-ohm real part, injection-locked amplification with locked gain vs frequency curves similar to Fig. VI-28 were obtained. The high degree of diode interchangeability in this circuit indicates that the TRAPATT phenomena may be very circuit dominated, while the high efficiency in the fixed-tuned circuit indicates that the 3rd may be as high a harmonic as need be considered for practical amplifiers.

## CHAPTER VII

### SUMMARY AND CONCLUSIONS

The TRAPATT mode of operation of avalanche diodes is a mechanism which can convert DC bias power to microwave frequencies at efficiencies which are quite high for solid-state devices. Reported efficiencies as high as 75 percent have been achieved, although more reproducible results are 20 to 40 percent for either free-running or injection-locked oscillators and 10 to 25 percent for stable finite bandwidth amplifiers. The high efficiency associated with this device is the result of quasi-rectangular voltage and current waveforms, which are necessarily high in harmonic content, and require appropriate terminating impedances from the circuit at several higher harmonics of the operating frequency. This requirement appears to constrain the ability to simultaneously achieve high-gain bandwidth products and high efficiency in amplifiers.

TRAPATT diodes are one-port negative-resistance devices which require some form of nonreciprocal device, such as a ferrite circulator, in order to separate input from output power when used as amplifiers.

The TRAPATT phenomena is an inherently large signal process, which requires some stimulus for oscillations to begin. Several theories have been proposed for the initiation of the mode, and present understanding of the transient behavior characterizing "turn-on" of the TRAPATT mode is limited. The mode is characterized by large depressions of the DC operating voltage from its zero-current bias level, permitting amplifiers to be operated in a class-C bias condition.

TRAPATT diodes are predominantly high-peak-power, short-pulse, low-duty-cycle devices, although a few CW results have been obtained. Significant government-sponsored development efforts have been expended to increase allowable pulse lengths and duty cycles at high peak power levels. The highest pulse energy reported to date is 0.005 J, corresponding to 50-W peak power in a 100- $\mu$ sec pulse. Device heating during long, high power pulses is not only a potential destruction mechanism, but thermal detuning before onset of failure causes further limitations on achievable-gain bandwidth products in amplifiers operated under such conditions.

It is doubtful that the highly nonlinear behavior of these devices will ever permit the simultaneous achievement of high peak power, long pulse length, wide bandwidth, high gain and efficiency, and simple enough circuit fabrication techniques, to make their use as phased-array power sources attractive for S-band BMD radar systems. Further support and development for this purpose appear unwarranted at this time, therefore. On the other hand, TRAPATT operation is a circuit-dominated phenomena which does appear attractive for applications in which narrowband, short pulse requirements would benefit from the existence of solid-state, moderate-voltage, class-C devices with efficiencies in the 30- to 40-percent range. Continued support by sponsors who have such requirements is considered worthwhile, particularly in the case of University-oriented systematic inquiry into and modeling of the basic device operating principles.

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APPENDIX  
GOVERNMENT CONTRACT REPORTS

A. INTRODUCTION

The open literature abounds with references to TRAPATT operation of microwave avalanche diodes, and many of the most important of these have been cited throughout this report. In addition, the interested researcher may profit from an examination of documentation generated by government-sponsored research contracts, and available through the National Technical Information Service. These are listed alphabetically by principal author in this appendix.

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14 TR-524

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

19 REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER 18 ESD-TR-77-30	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) 6 Theory and Operating Characteristics of TRAPATT Amplifiers		5. TYPE OF REPORT & PERIOD COVERED 9 Technical Report
7. AUTHOR(s) 10 Richard W. Laton, Martin I. Grace George I. Haddad		6. PERFORMING ORG. REPORT NUMBER Technical Report 524 ✓
9. PERFORMING ORGANIZATION NAME AND ADDRESS Lincoln Laboratory, M.I.T. P.O. Box 73 Lexington, MA 02173		8. CONTRACT OR GRANT NUMBER(s) 15 F19628-76-C-0002
11. CONTROLLING OFFICE NAME AND ADDRESS Ballistic Missile Defense Program Office Department of the Army 5001 Eisenhower Avenue Alexandria, VA 22333		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 76 Project No. 8X36334D215
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) Electronic Systems Division Hanscom AFB Bedford, MA 01731		12. REPORT DATE 11 26 Jan 1977
		13. NUMBER OF PAGES 74 1269 p.
		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Distribution limited to U.S. Government agencies only; test and evaluation; 9 June 1977. Other requests for this document must be referred to ESD/TML (Lincoln Laboratory), Hanscom AFB, MA 01731.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES None		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)		
TRAPATT IMPATT microwave power solid-state devices	power amplifiers negative resistance class-C amplifier phased-array radar	plated heat sink distributed area diodes cruciform diode
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) This report describes the current state of understanding of the theory and operating characteristics of microwave avalanche diodes operating in the TRAPATT mode as both oscillators and amplifiers. Device operating principles, and their dependence upon material, impurity profile, structure, biasing and circuit loading, are described. Methods of device fabrication are discussed, and present state of the art is tabulated for oscillators and amplifiers on a power-frequency basis. Techniques developed for the design of TRAPATT amplifiers as a result of several programs sponsored by the U.S. Army Ballistic Missile Defense Advanced Technology Center are discussed, and experimental results (primarily at S-band) are presented.		

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